

# **Measuring Material Properties to Build Material Models in FEA**

Kurt Miller

[www.axelproducts.com](http://www.axelproducts.com)

# Who is Axel Products, Inc.

## Physical Testing Services for Engineering and Analysis

The testing images and data sets were created in the Axel Products laboratory. The testing methods discussed are available as a service to analysts around the world.

For additional information, visit us at:  
**[www.axelproducts.com](http://www.axelproducts.com)**



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[Directions and Map](#)

[About Axel](#)

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## Physical Testing Services for Engineering and Analysis

### Training

**ABAQUS** [Testing and Analysis of Elastomers with ABAQUS](#)  
October 3-5, 2000.



### Technical Information

1. "Compression or Biaxial Extension?" ([PDF: 304 KB / 3 pages](#)).
2. "Measuring the Dynamic Properties of Elastomers for Analysis": ([PDF: 834 KB / 7 pages](#)).
3. "Testing Elastomers for Hyperelastic Material Models in Finite Element Analysis": ([PDF: 775 KB / 8 pages](#)).

[more...](#)

### Testing Services

#### [Hyperelastic Properties of Elastomers](#)

<i>Experiments:</i>	<i>Data for:</i>
Simple Tension	Ogden
Pure Shear	Mooney-Rivlin
Equal Biaxial	Arruda-Boyce
Compression & Volumetric	Damage Models
	Viscoelastic Decay



#### [Elastic-Plastic Properties of Plastics](#)

<i>Experiments:</i>	<i>Data for:</i>
Modulus	
Poisson's Ratio	



# A Strategy for Material Model Development

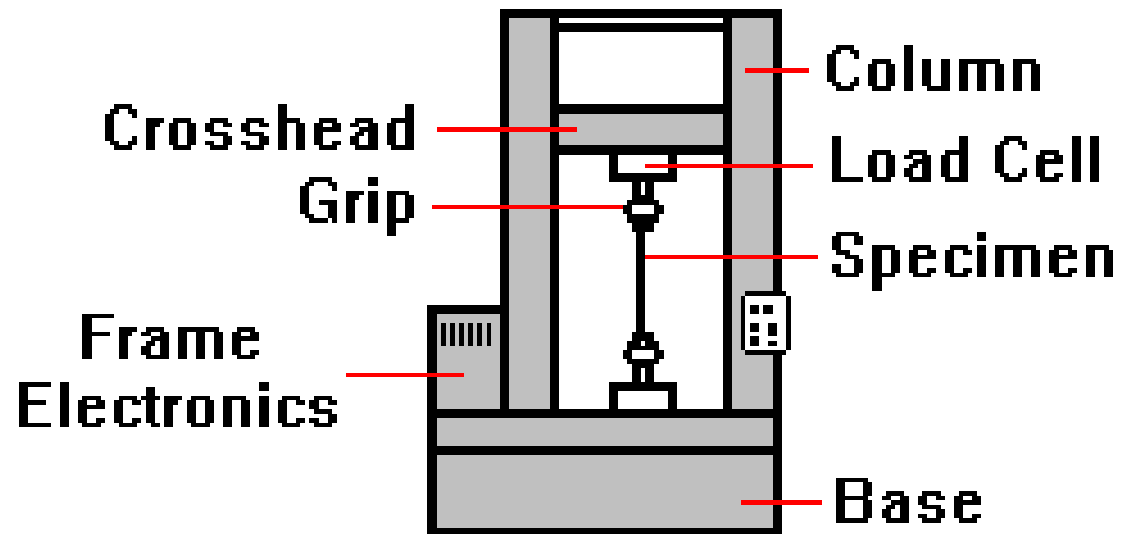
- ❑ Understand the Loading Conditions of the Part
- ❑ Understand the General Behavior of the Materials Involved
- ❑ Select the Material Behaviors Significant to the Simulation Effort
- ❑ Use Existing or Develop Material Models to Describe the Behavior
- ❑ Verify the Performance of the Material Model

# Understanding the General Behavior of the Materials Involved

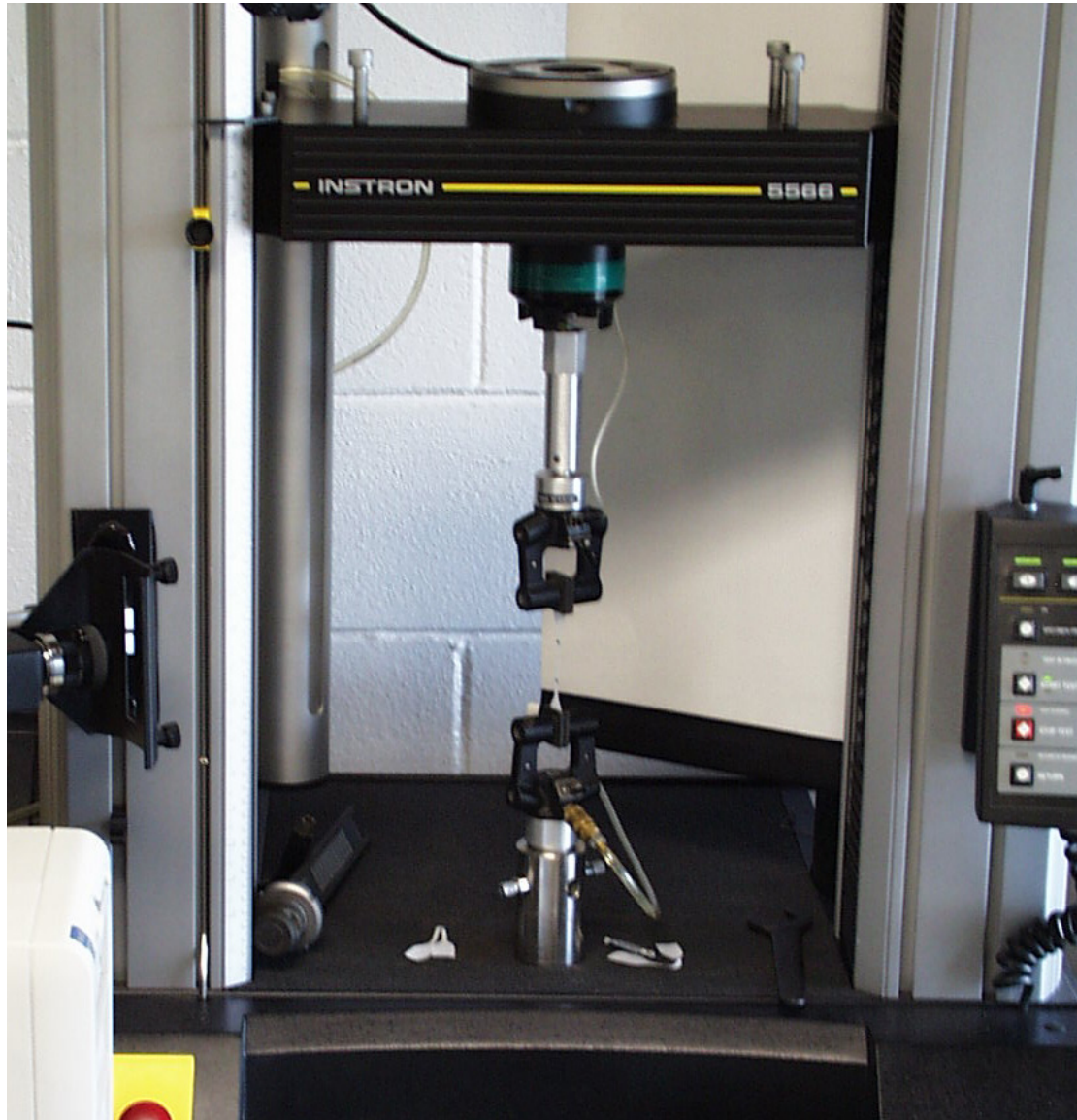
- ☐ Static Behavior
  - Plastics
  - Elastomers
- ☐ Temperature
- ☐ Dynamic Loadings
  - Rate
  - Noise and Vibration
- ☐ Fatigue and Aging

# Static Behavior

## Load Frame

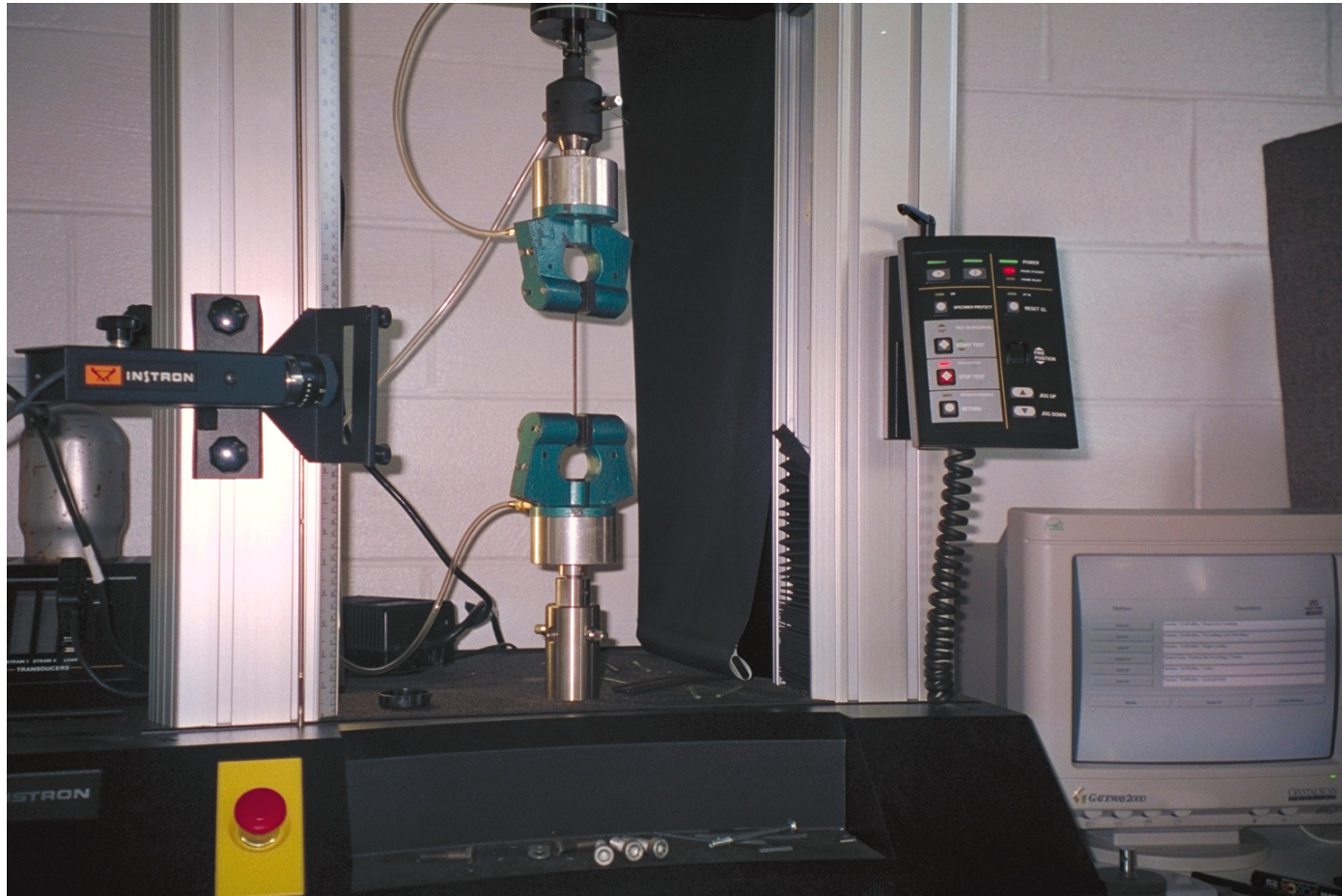


# Static Behavior

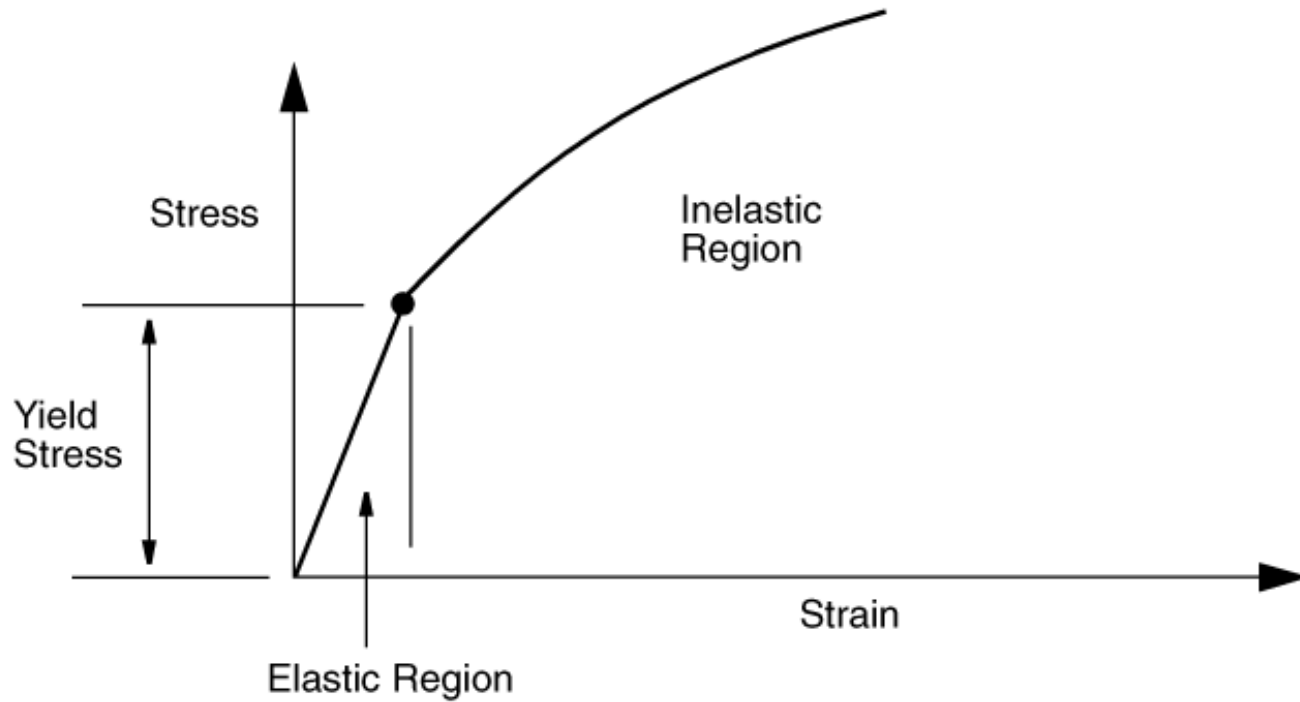




# Static Behavior



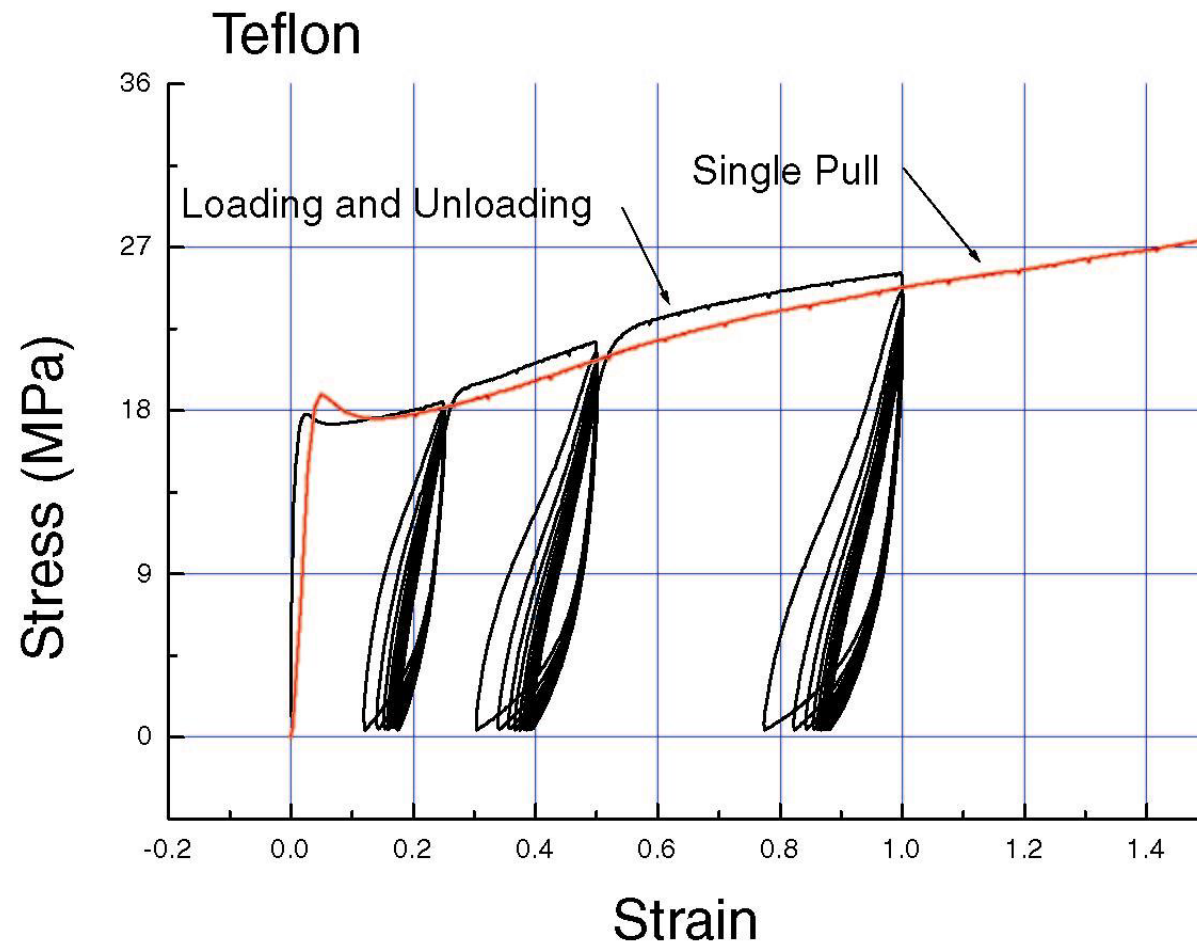
# Static Behavior



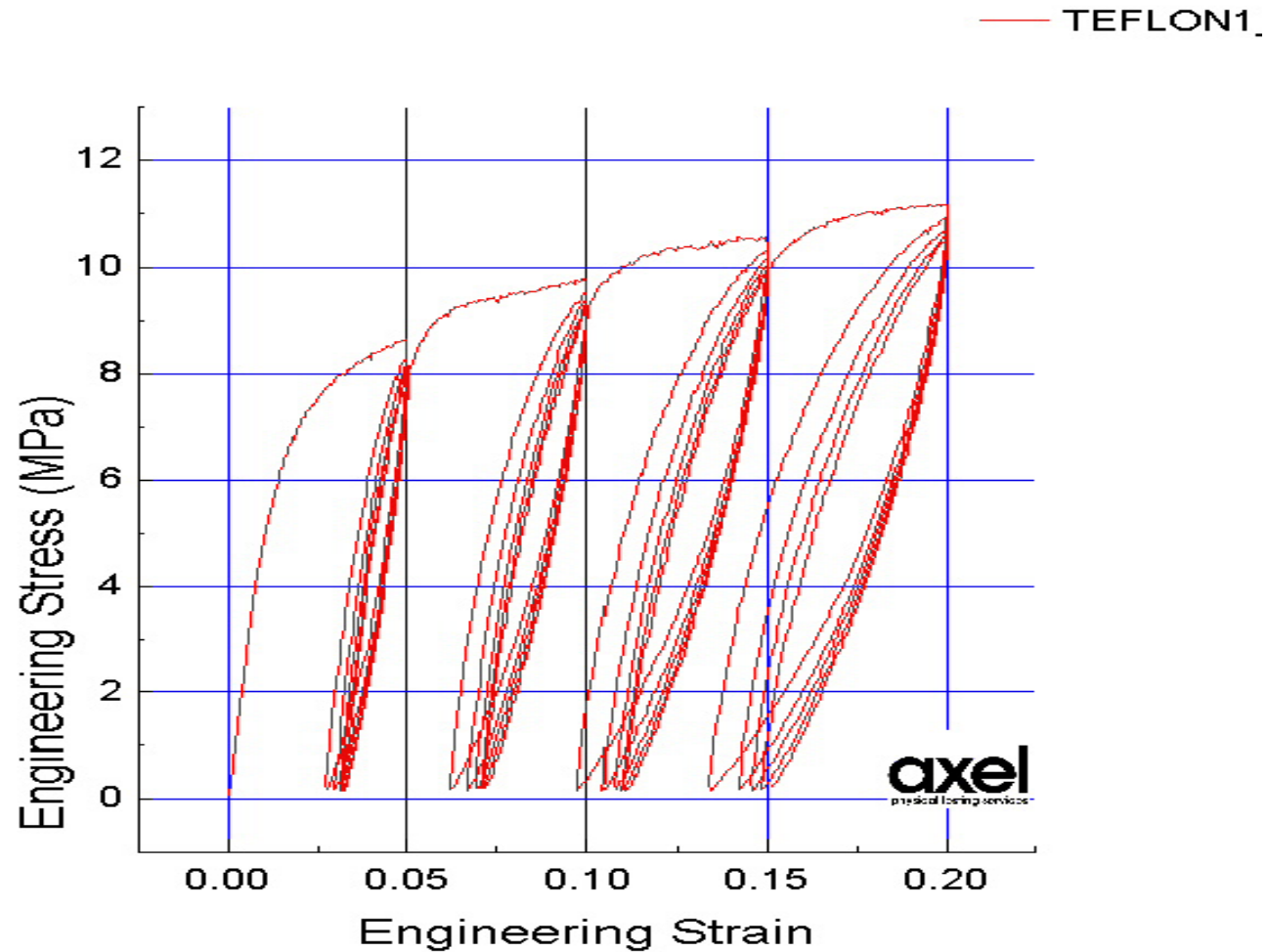
**Note:** Stress and strain are total quantities.



# Static Behavior



# Static Behavior

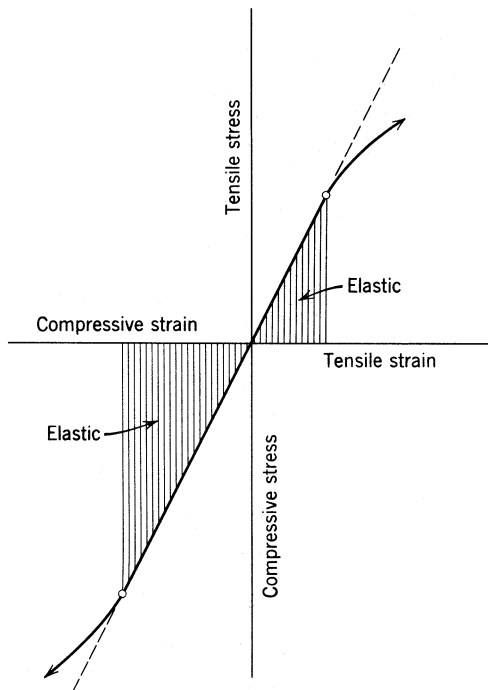


# Static Behavior

## Comparison of Metal Response to that of Rubber

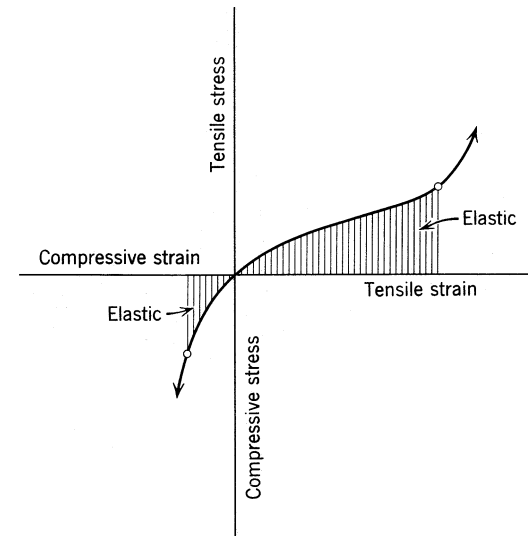
### Crystalline Solid

Small elastic strain (.2%)  
Plastic yielding  
Tension / Comp. Similar



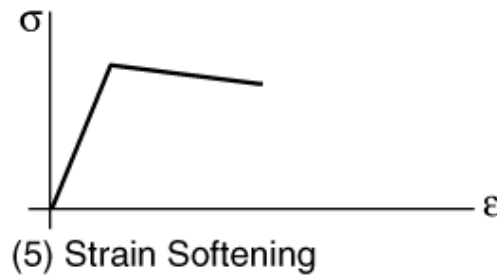
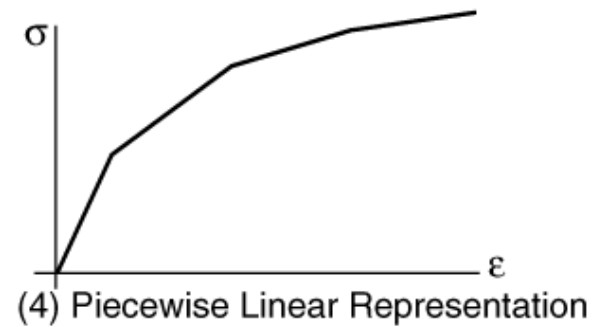
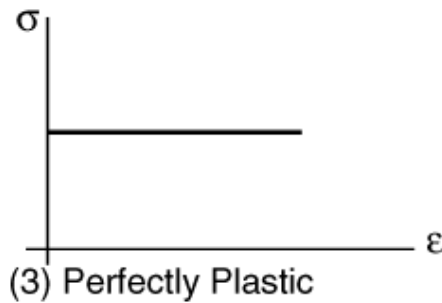
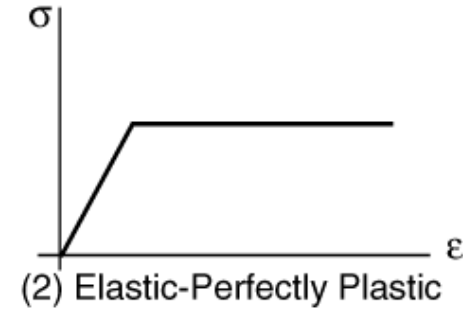
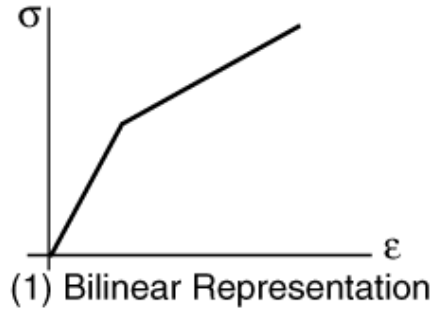
### Rubber

Large Elastic Strains (600%)  
Complex Damage  
Tension / Comp very different  
Viscoelastic, Hysteresis



# Static Behavior

## Simple Models



Meaningful Parameters:  
Young's Modulus,  $E$   
Poisson's Ratio,  $\nu$

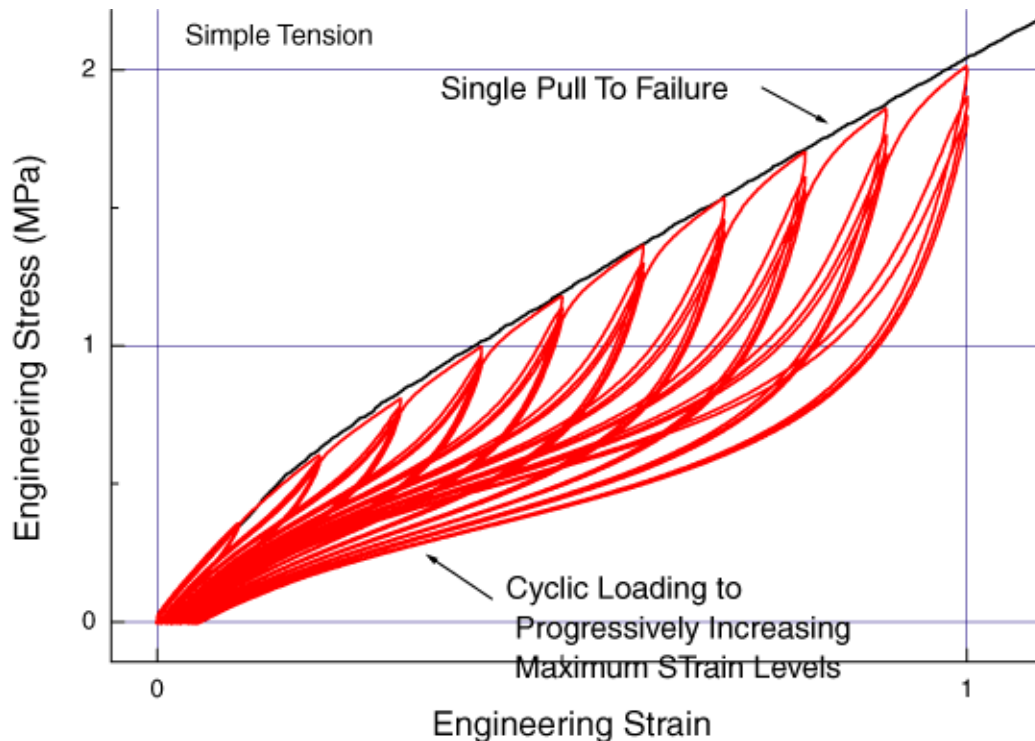
Simplified Stress-Strain Curves (Uniaxial Test)

# Static Behavior

## Elastomer Behavior, Typical Stress-Strain Response

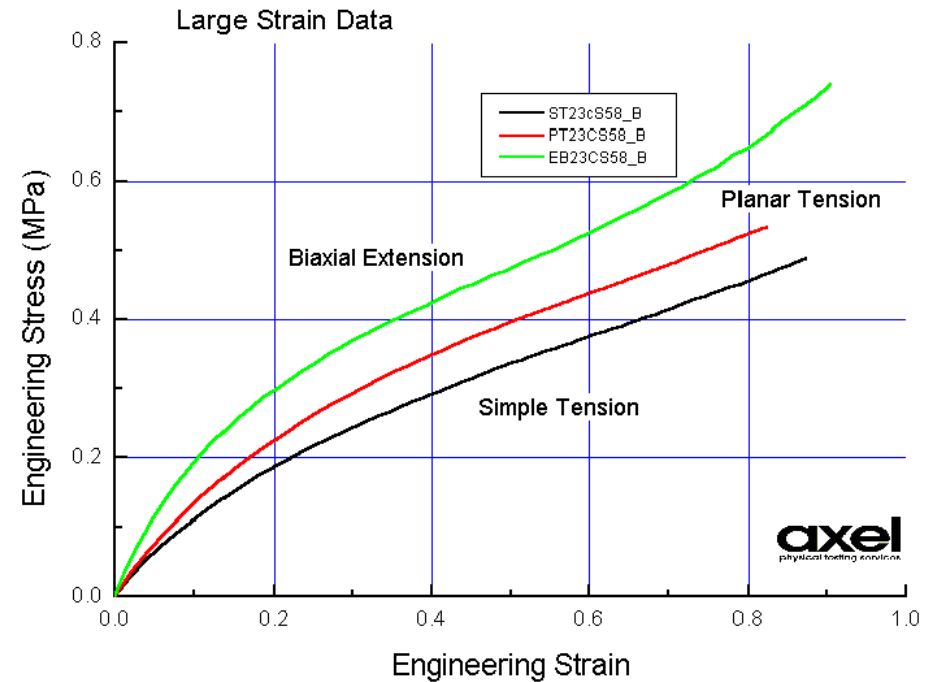
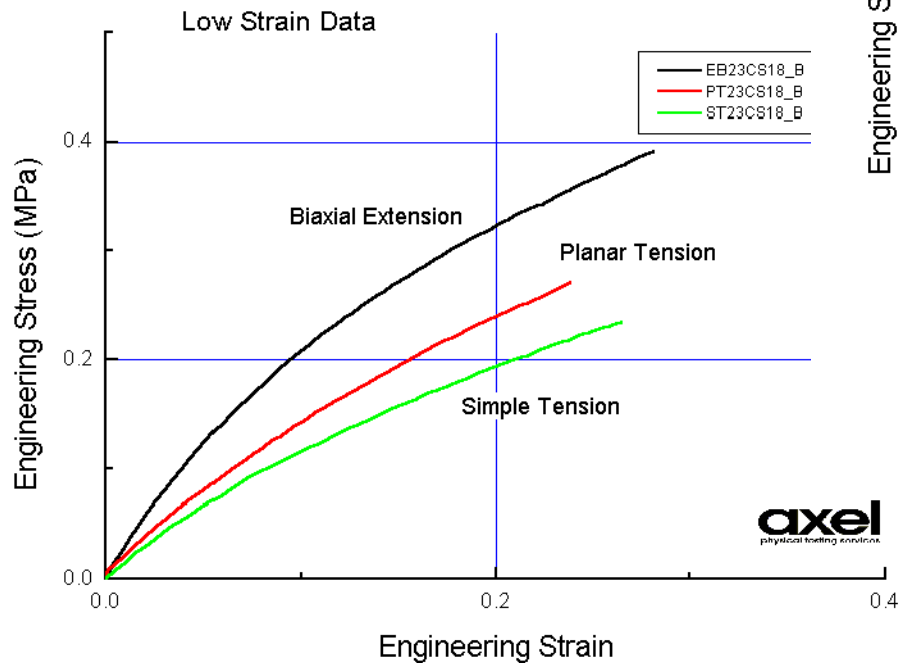
Load, unload cycles show hysteresis and damage

Progressive loads shows progressive damage



**Non-physical Parameters:**  
(i.e., non-measurable) coefficients of nonlinear functions of strain—Must be automatically calibrated (i.e., curve fit) from test data.

# Strain States



## Pure States of Strain or Stress

- ☐ Simple Tension
- ☐ Pure Shear
- ☐ Simple Compression, Biaxial Extension
- ☐ Bulk Compression



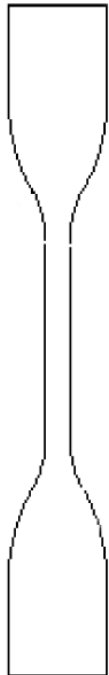
# Tensile Testing in the Lab

What is Simple Tension?

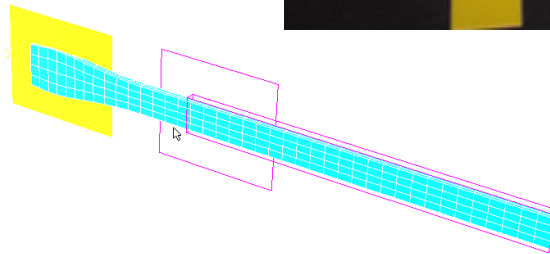
Uniaxial Loading

Free of Lateral

constraint



Gage Section:  
Length:Width  
>10:1



# Tensile Testing in the Lab

Measure Strain only in the Region where a Uniform State of Strain Exists

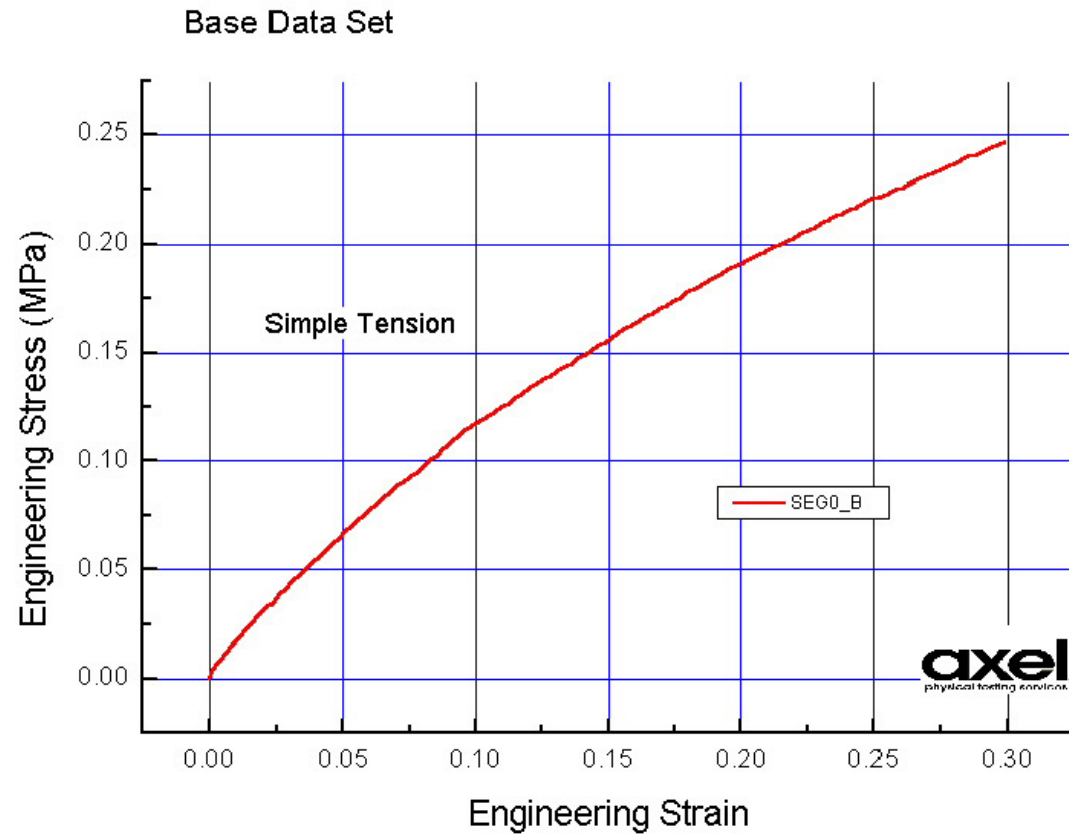
No Contact



# Tensile Testing in the Lab

Initial Loading

Typical of Data from  
Existing Standards

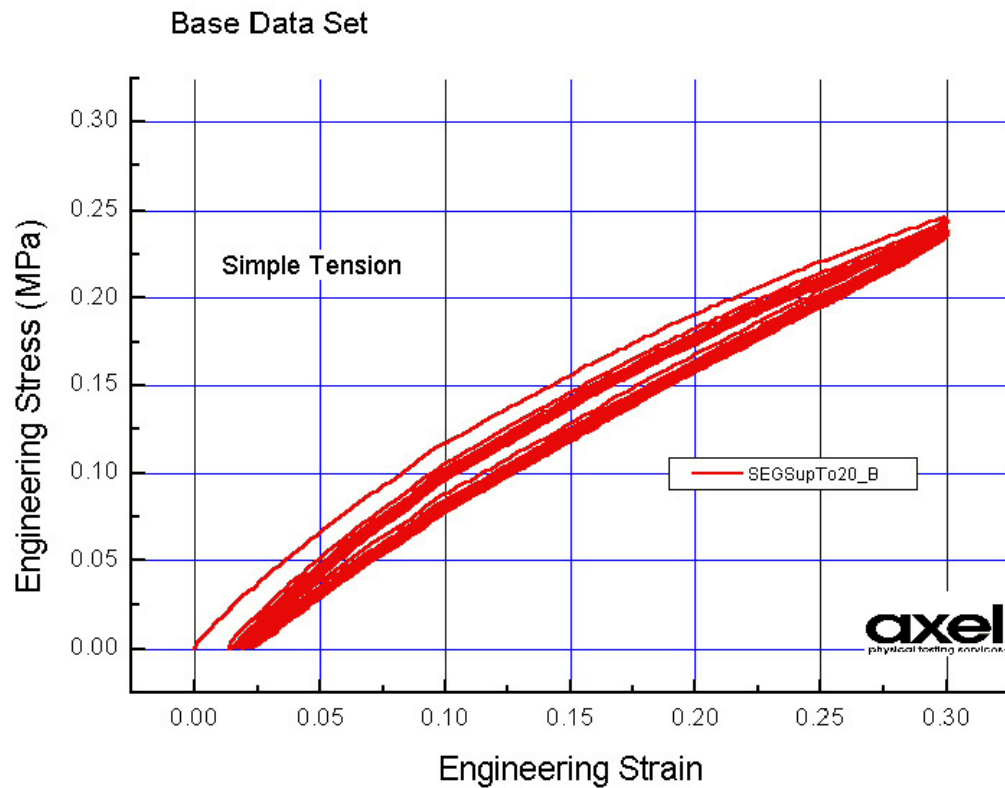


# Tensile Testing in the Lab

Multiple Loadings

Softening

Permanent Strain Effects

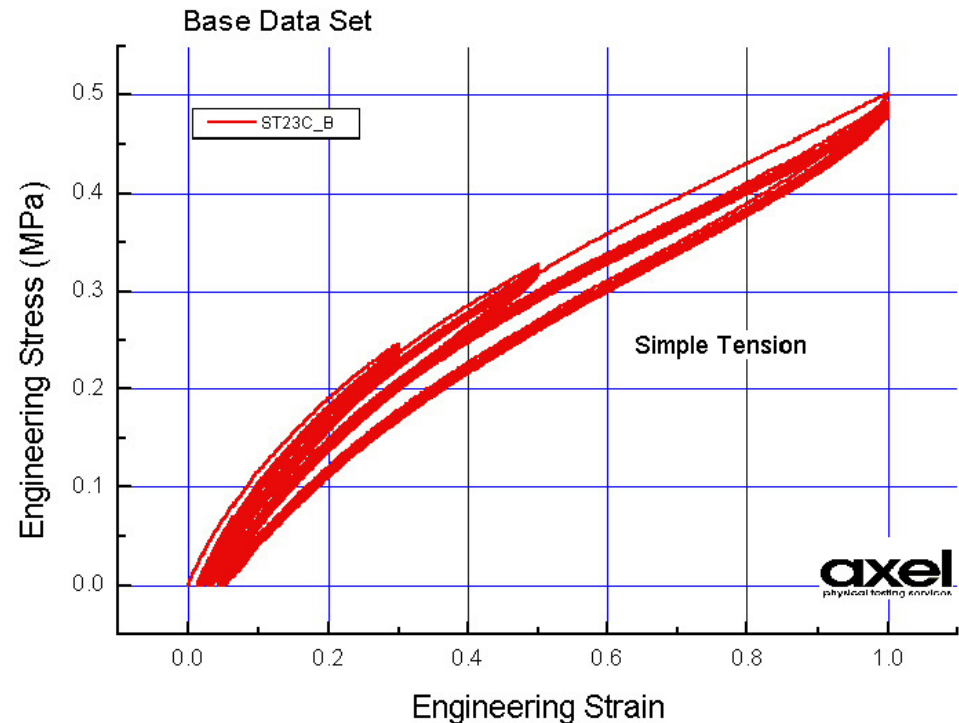


# Tensile Testing in the Lab

Loading to Larger Strain Levels

Additional Softening

Additional Permanent Damage



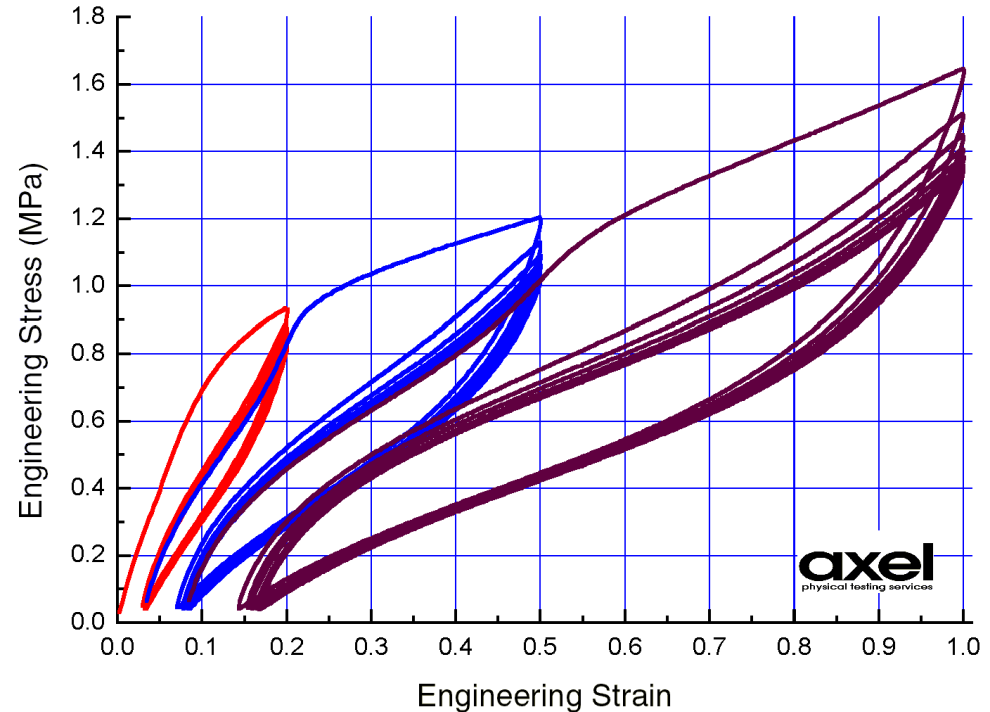
# Tensile Testing in the Lab

Some Common Elastomers Exhibit Dramatic Strain Amplitude and Cycling Effects at Moderate Strain Levels

## Conclusions:

Test to Realistic Strain Levels

Use Application Specific Loadings to Generate Material Data

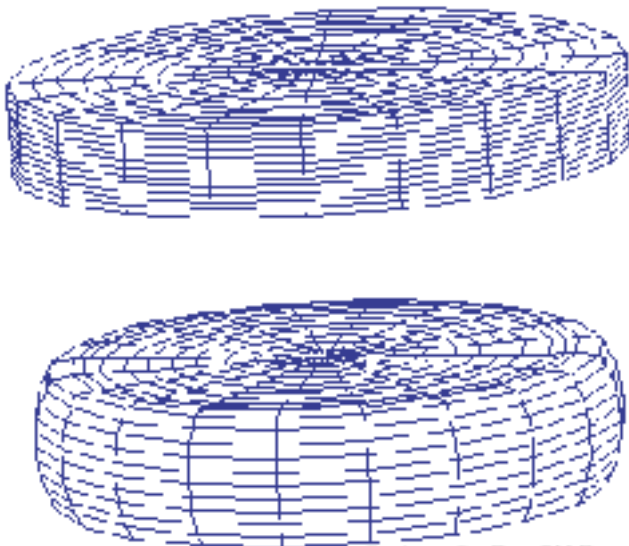


# Compression Testing in the Lab

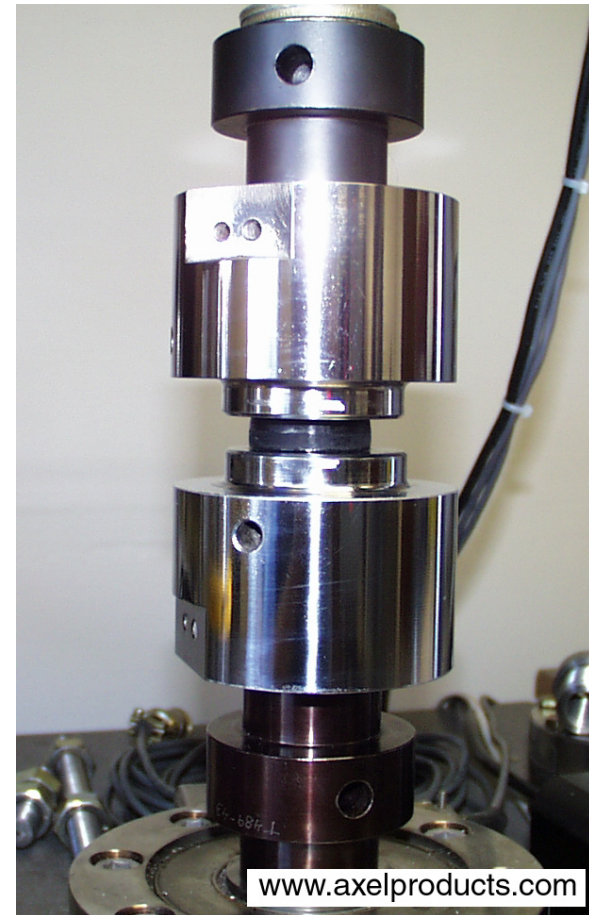
## Requirements:

Uniaxial Loading

No Lateral Constraint



Courtesy, Jim Day, GM Powertrain



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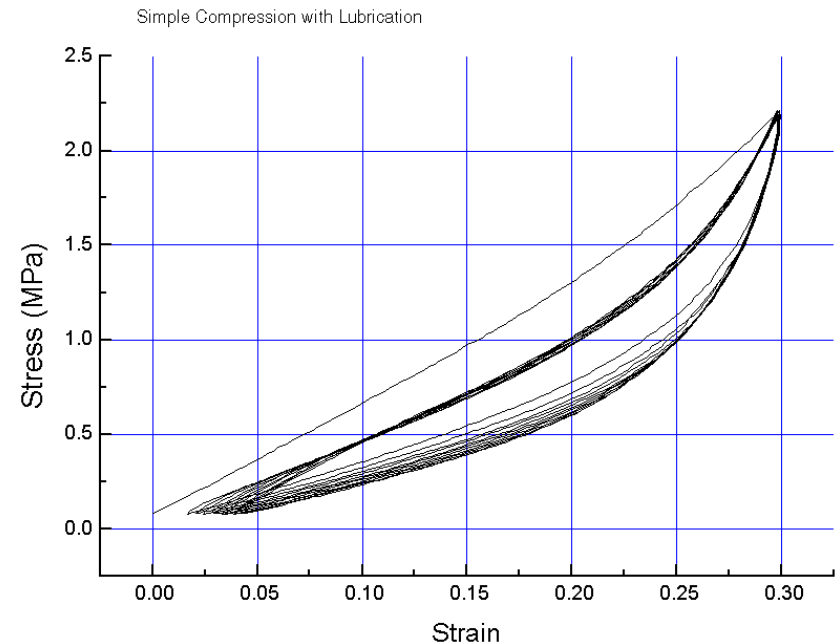
# Compression Testing in the Lab

It is Experimentally Difficult to Minimize Lateral Constraint due to Friction at the Specimen Loading Platen Interface

Friction Effects Alter the Stress-strain Curves

The Friction is Not Known and Cannot be Accurately Corrected

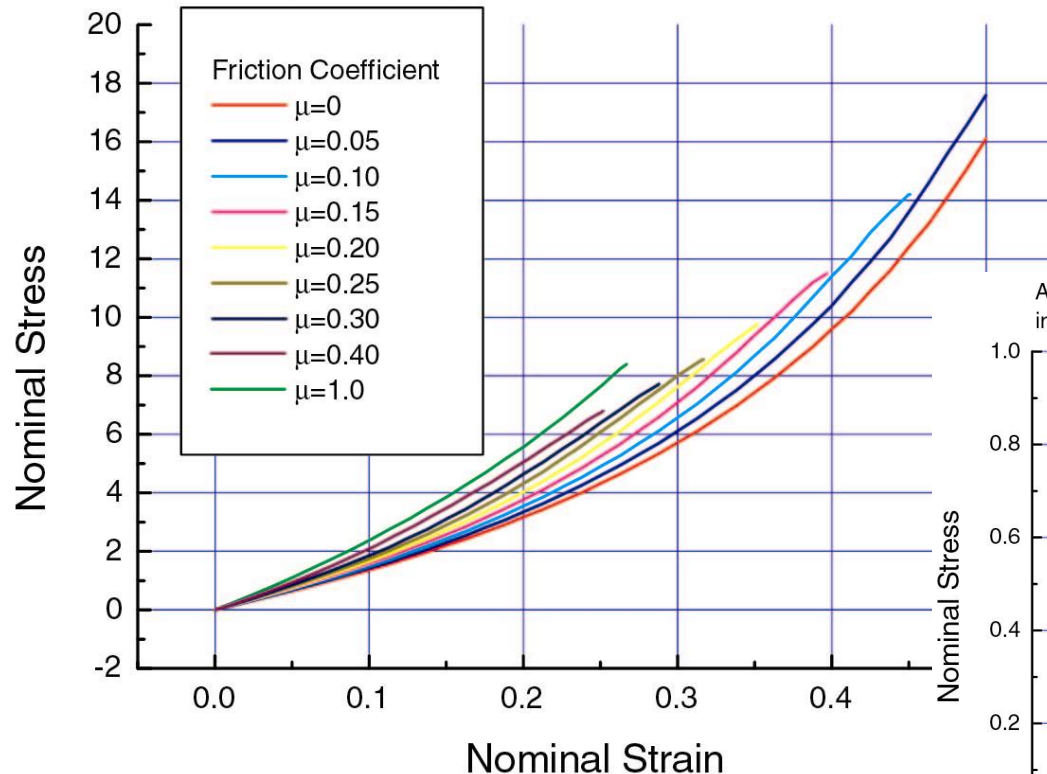
Even Very Small Friction Levels have a Significant Effect at Very Small Strains



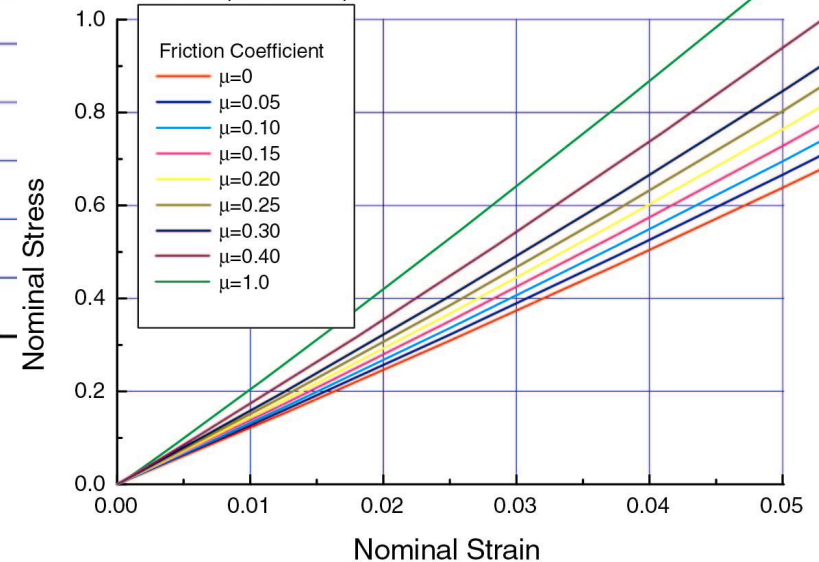
# Compression Testing in the Lab

## Friction Effects on Compression Data

An Analytical Analysis of the Effect of Specimen-Platen Friction in the Compression Experiment



An Analytical Analysis of the Effect of Specimen-Platen Friction in the Compression Experiment at Small Strains



Analysis by Jim Day, GM Powertrain

# Equal Biaxial Testing

## Why?

Same Strain State as  
Compression

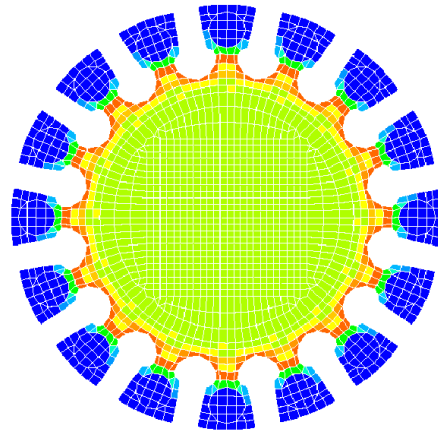
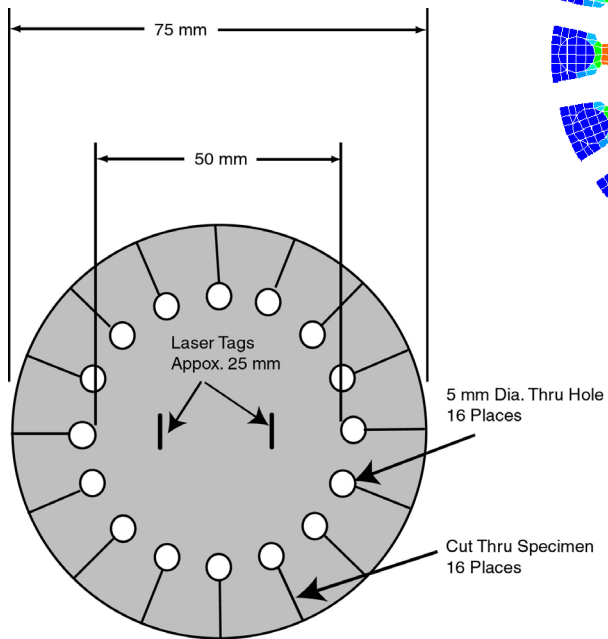
Can Not Do Pure Compression

Can Do Pure Biaxial

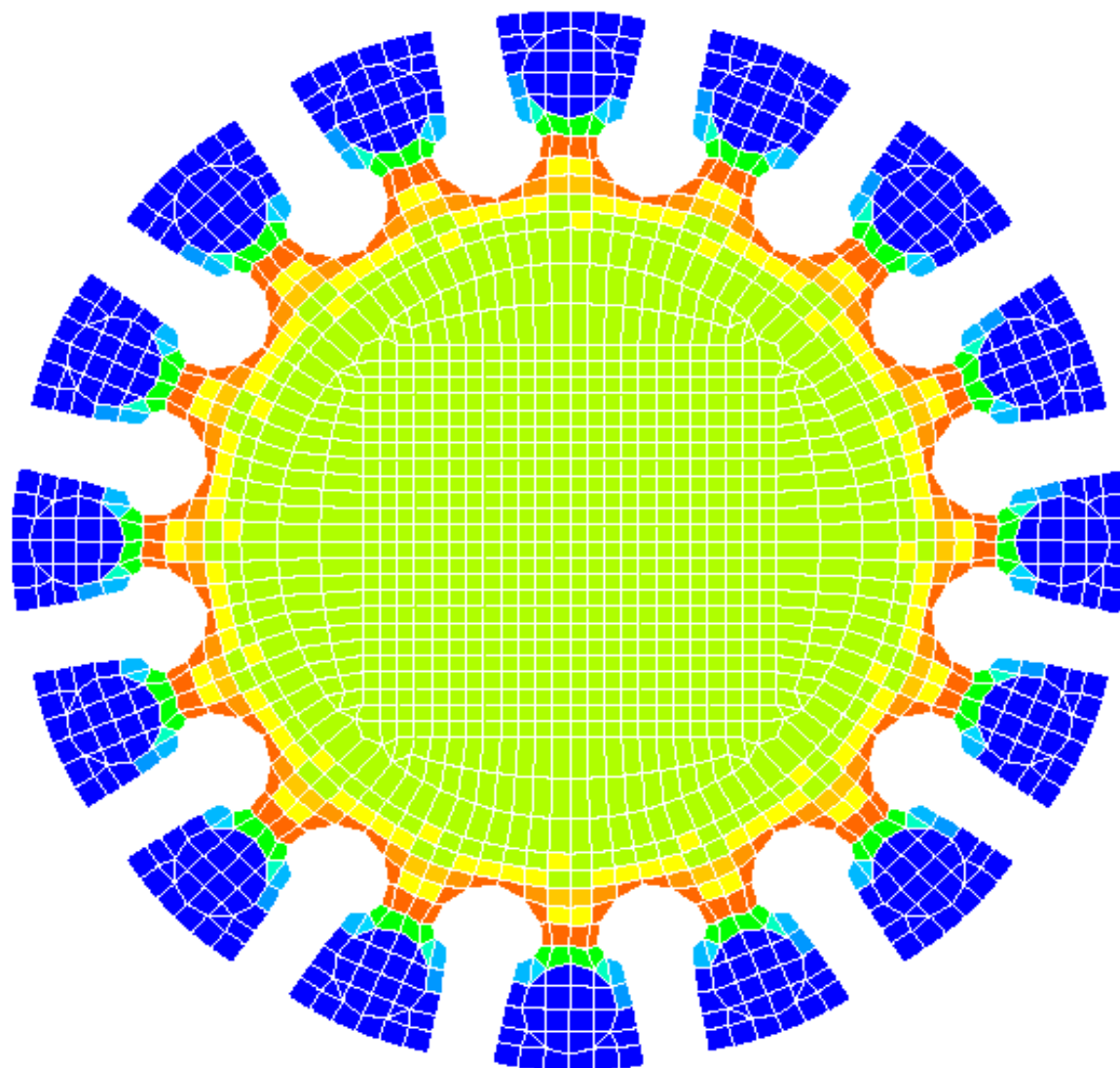
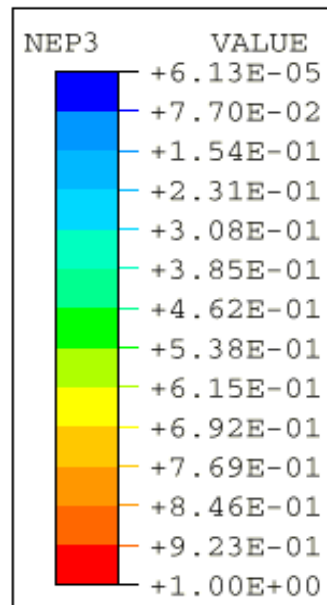


# Equal Biaxial Testing

Analysis of the Specimen Justifies  
Geometry







2  
3 1

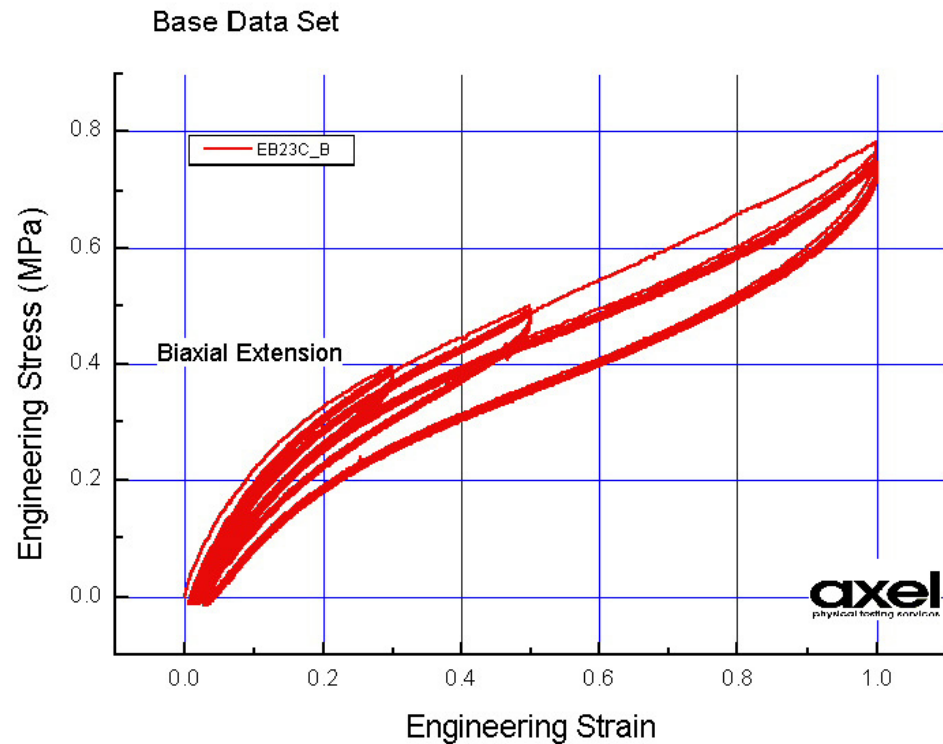
# Equal Biaxial Testing

Biaxial Extension

Curves have the same

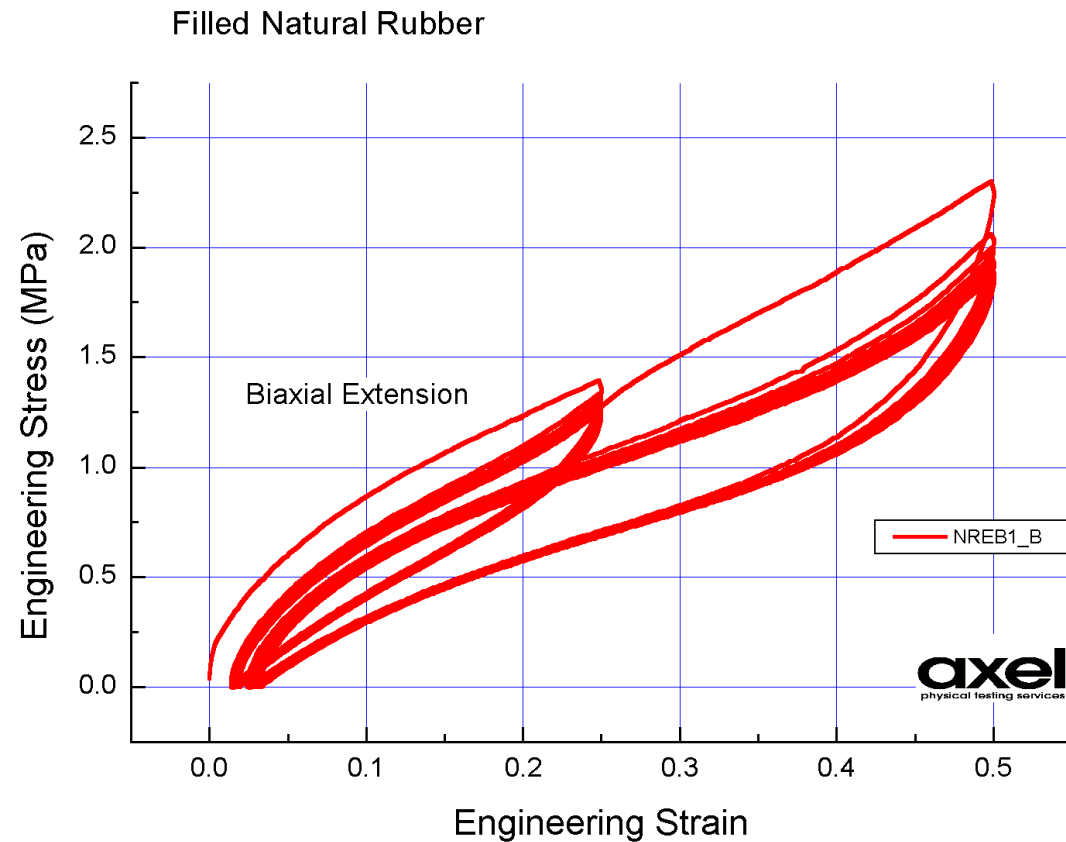
General Shape as  
Simple Tension

Allows for Matched  
Loading Conditions



# Equal Biaxial Testing

Some Common Elastomers Exhibit Dramatic Strain Amplitude and Cycling Effects at Moderate Strain Levels

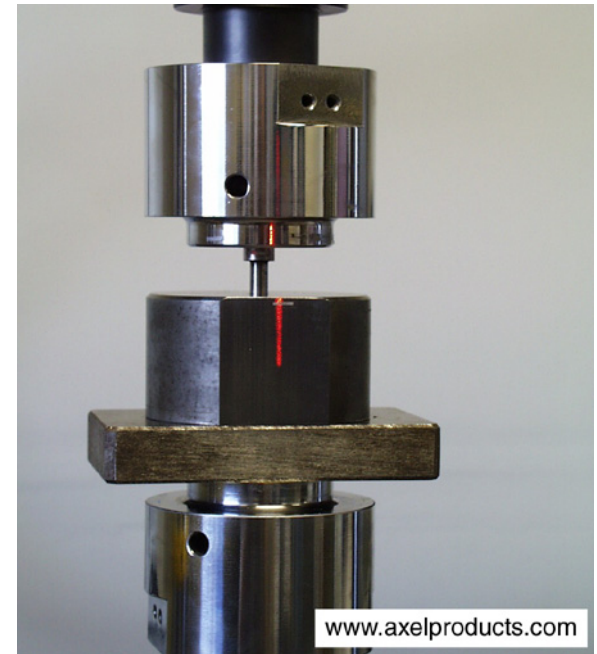
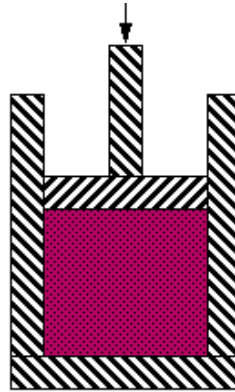




# Volumetric Compression Testing

**Direct Measure of the  
Stress Required to  
Change the Volume of  
an Elastomer**

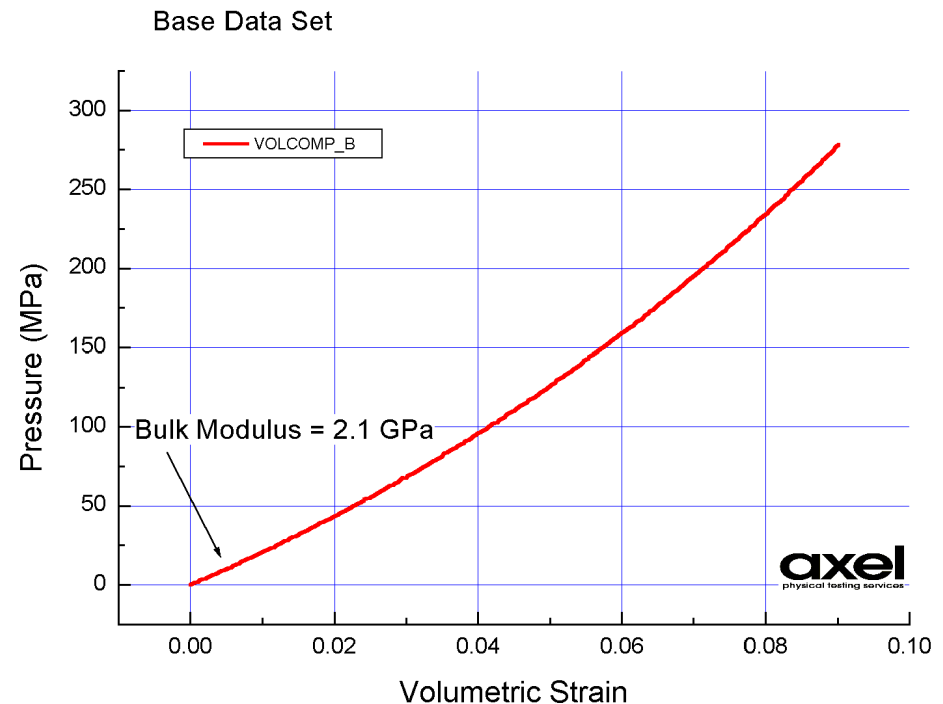
Requires Resolute  
Displacement Measurement  
at the Fixture



# Volumetric Compression Testing

Initial Slope = Bulk  
Modulus

Typically, only highly constrained applications require an accurate measure of the entire Pressure Volume relationship.



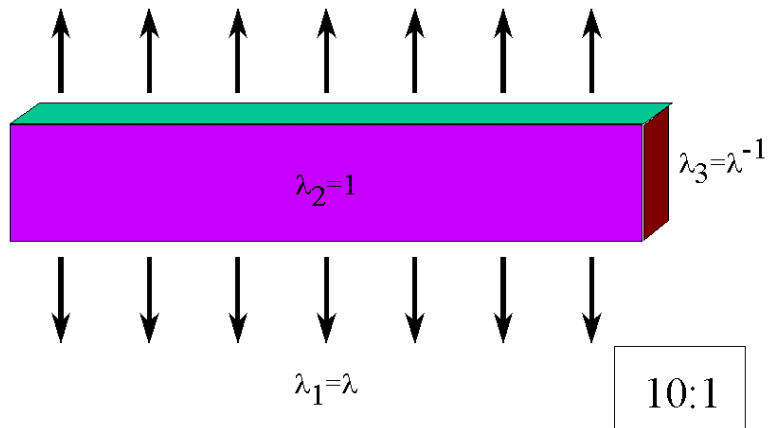
# Planar Tension Testing

## What is Planar Tension?

Uniaxial Loading

Perfect Lateral Constraint

All Thinning Occurs in One  
Direction



# Planar Tension Testing

Strain Measurement is  
Particularly Critical  
Some Material Flows  
from the Grips  
The Effective Height is  
Smaller than Starting  
Height so  $>10:1$   
Width:Height is  
Needed

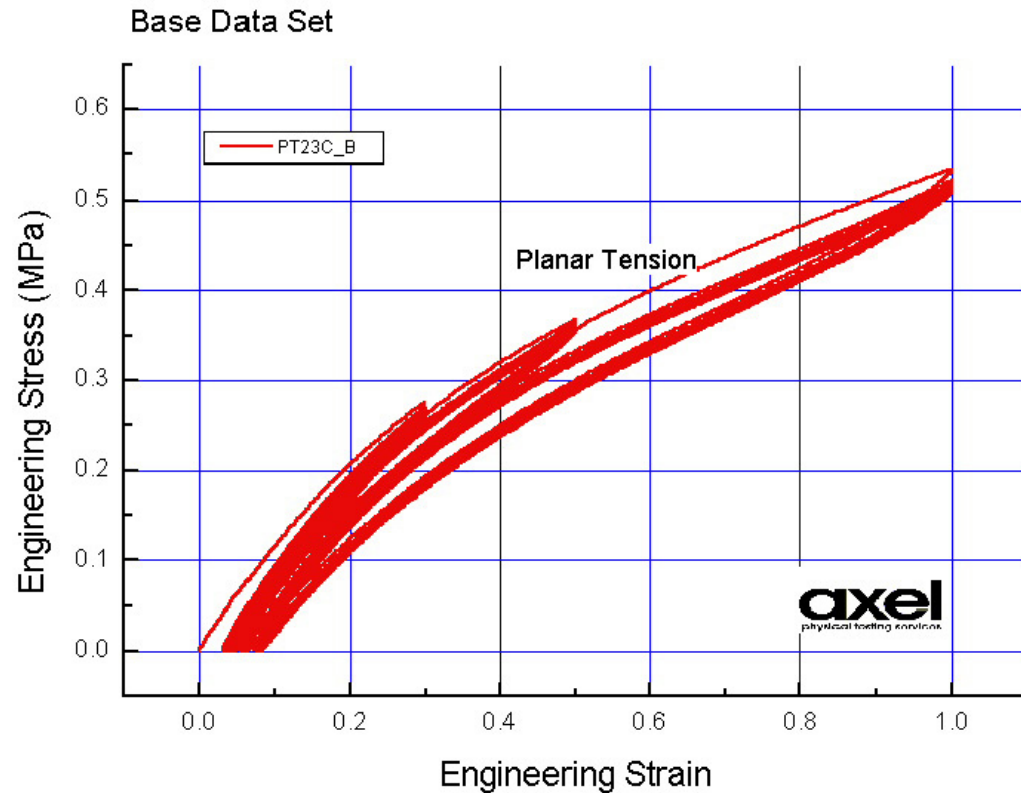


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# Planar Tension Testing

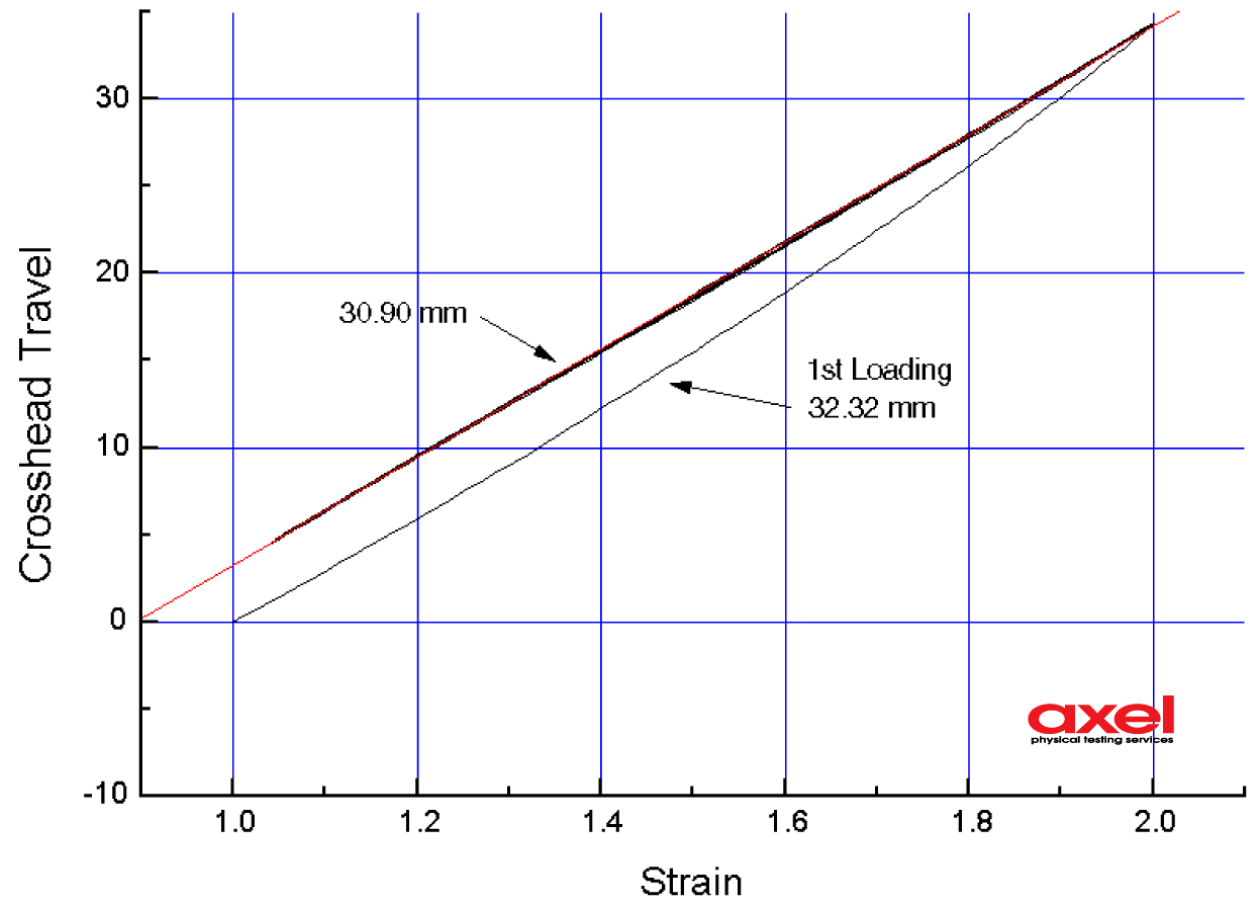
Similar Stress-strain Shape to  
Simple Tension and  
Biaxial Extension

Match Loadings between  
Strain States

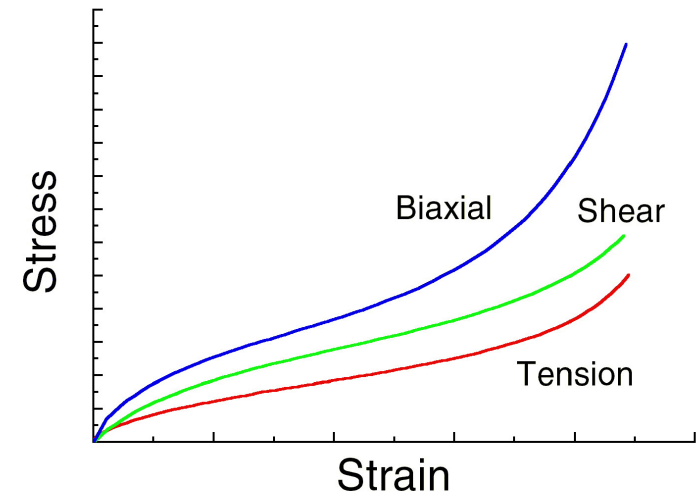
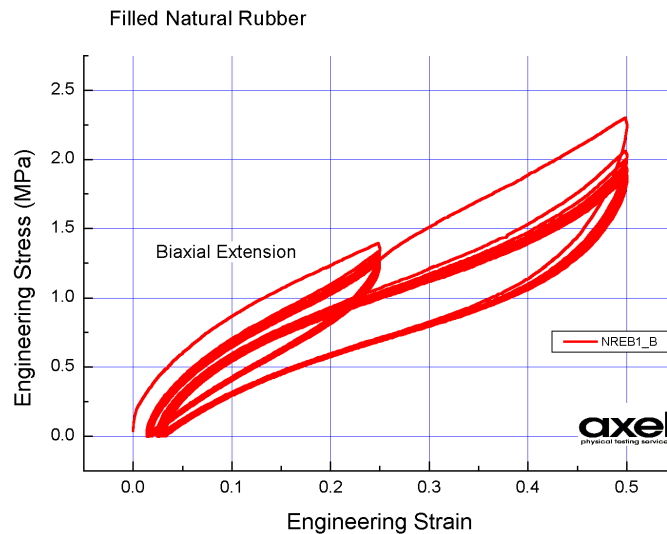


# Planar Tension Testing

A Small but Significant  
amount of Material  
will Flow From the  
Planar Tension Grips.

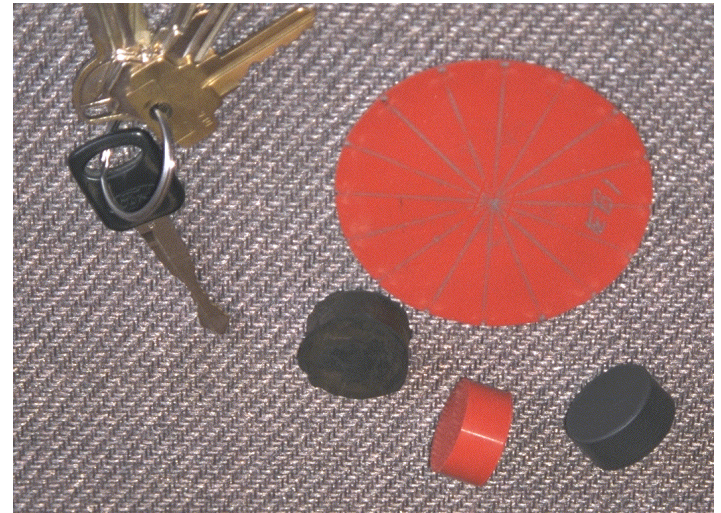
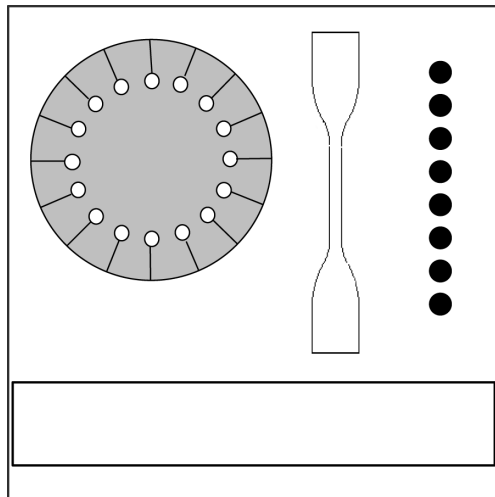
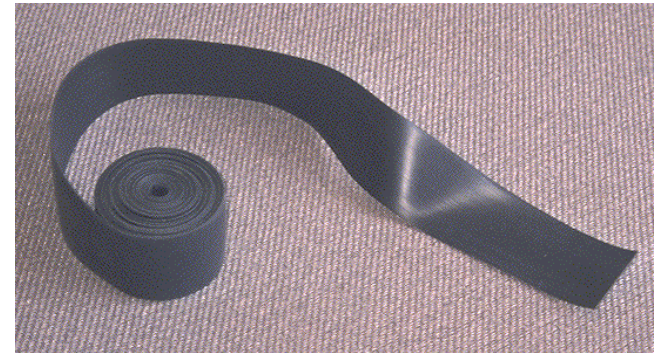
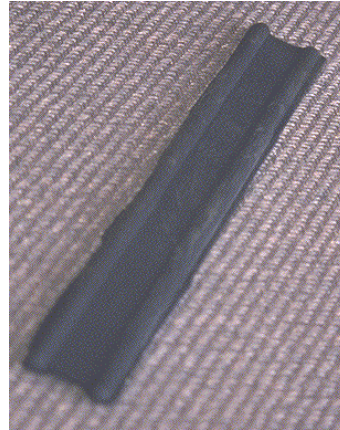
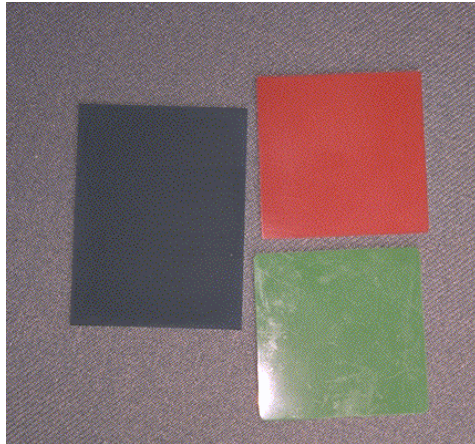


# Data Reduction in the Lab





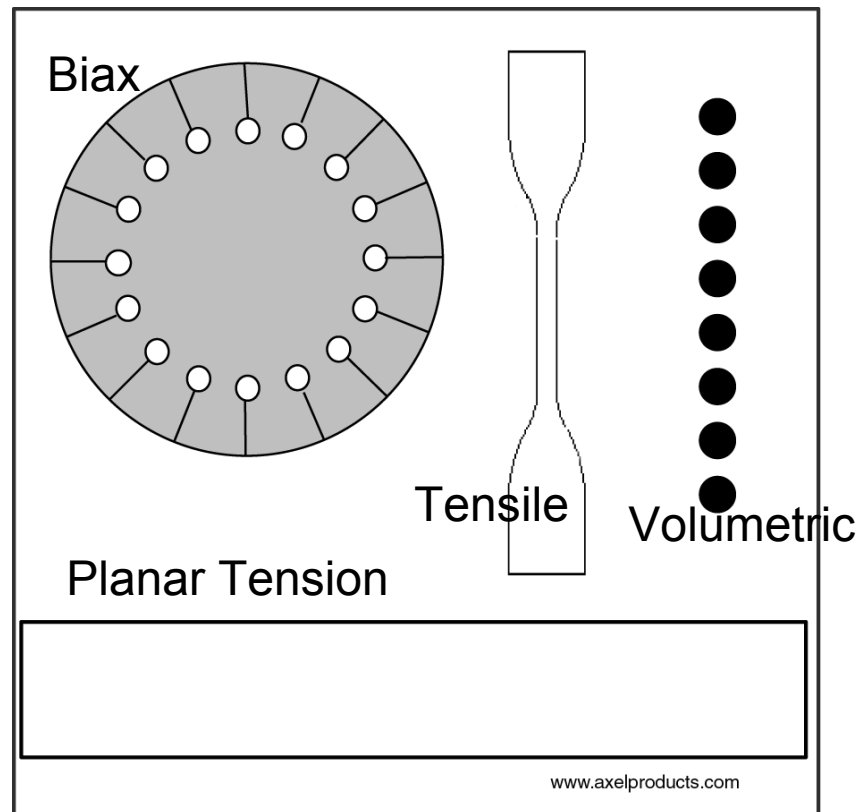
# Testing the Correct Material



# Testing the Correct Material

Consistent within The Experimental Data Set

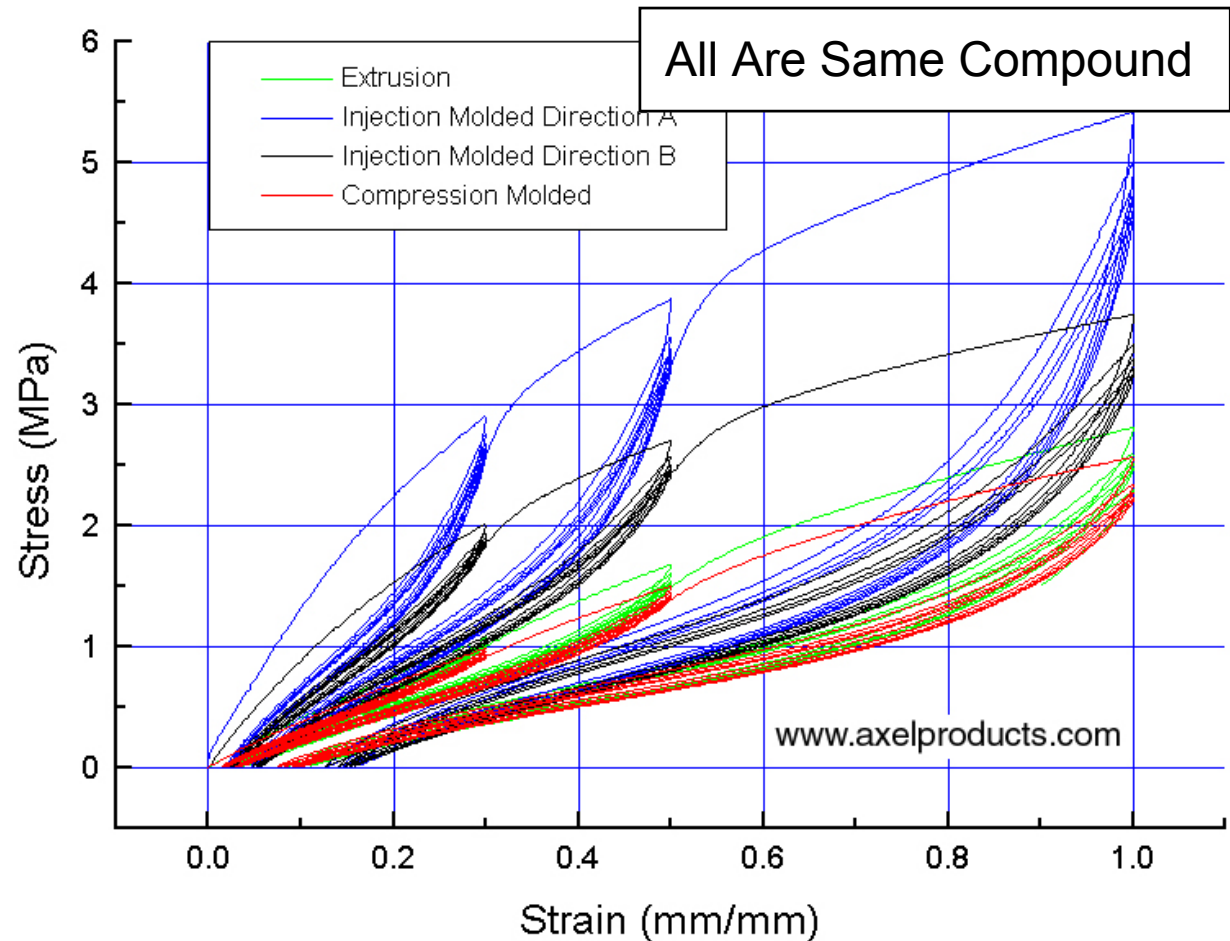
Cut All Specimens from the Same Slab



# Testing the Correct Material

Verify that The Tested Material is the Same as the Part

**Processing**  
**Color**  
**Cure**  
**History ...**



# Testing at Non-ambient Temperatures

Testing at the Application  
Temperature

Measure Strain at the Right Location

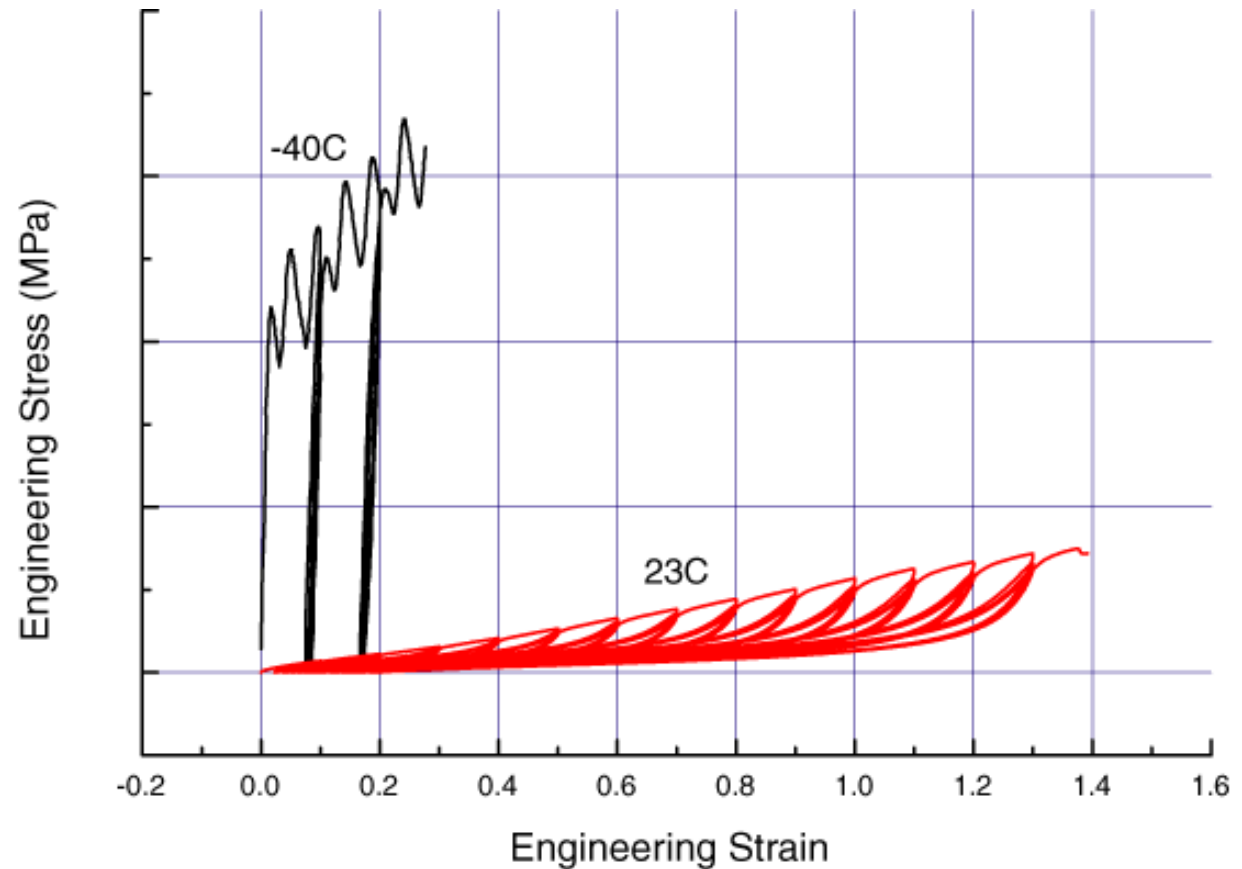
Perform Realistic Loadings





# Testing at Non-ambient Temperatures

Elastomers Properties Can Change by Orders of Magnitude in the Application Temperature Range.

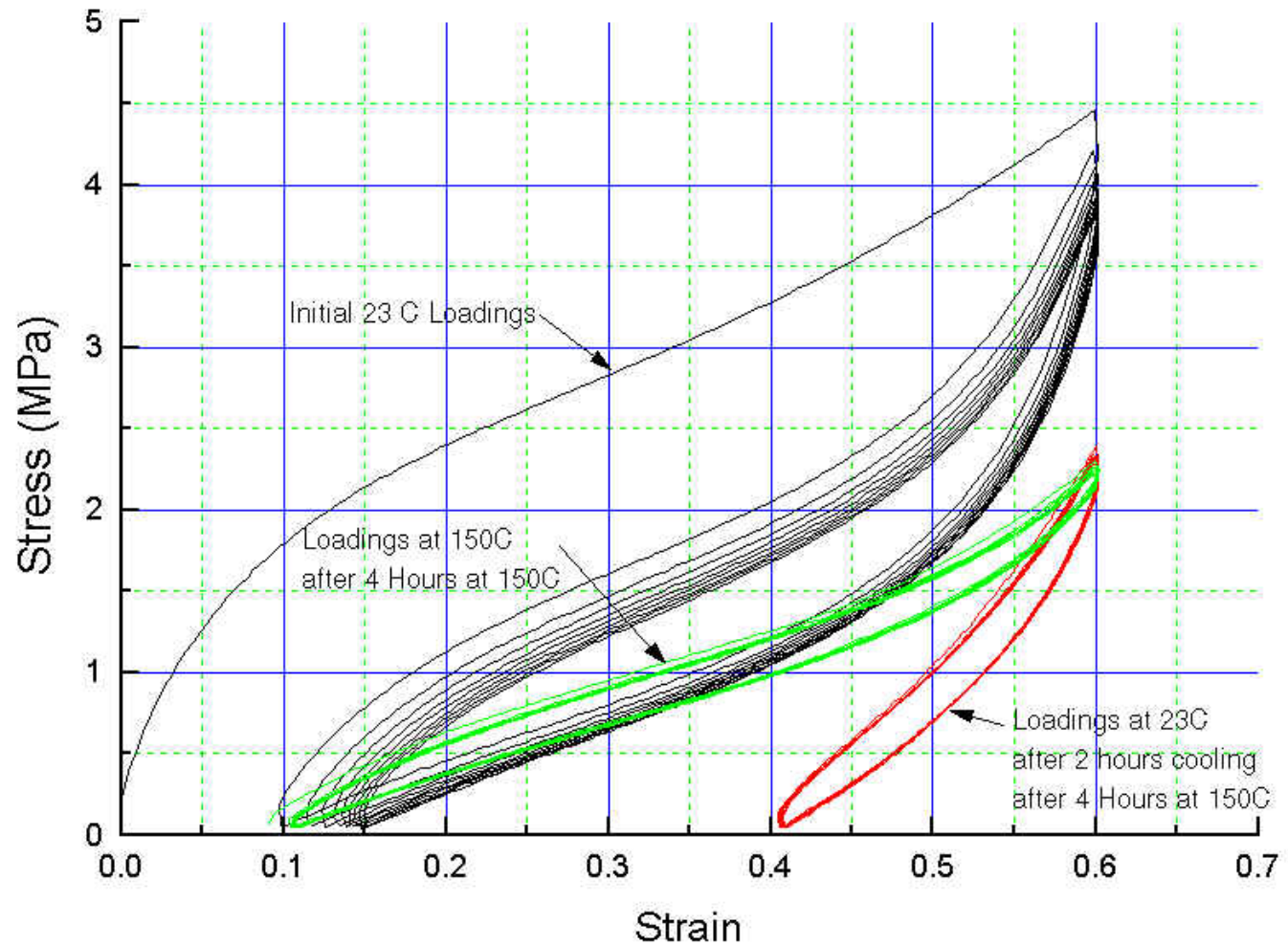


# Measuring Thermal Constants

- ☐ Thermal Conductivity
- ☐ Thermal Diffusivity
- ☐ Specific Heat

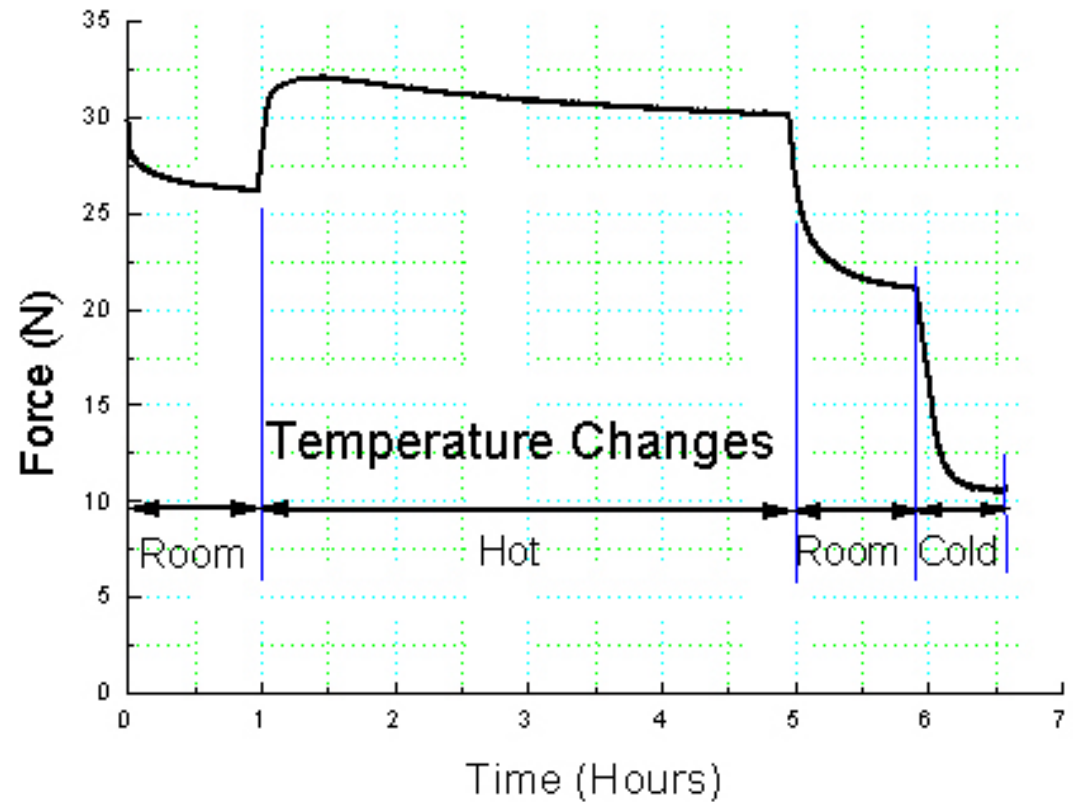
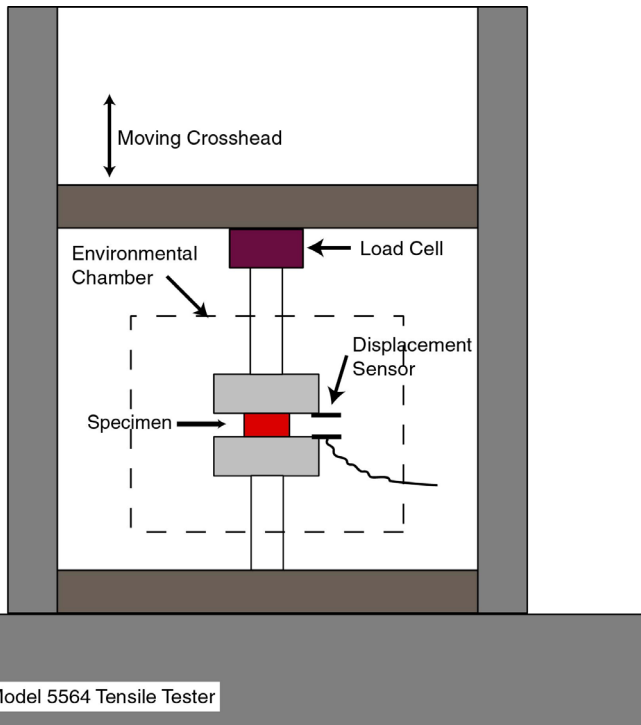


# Thermal Effects

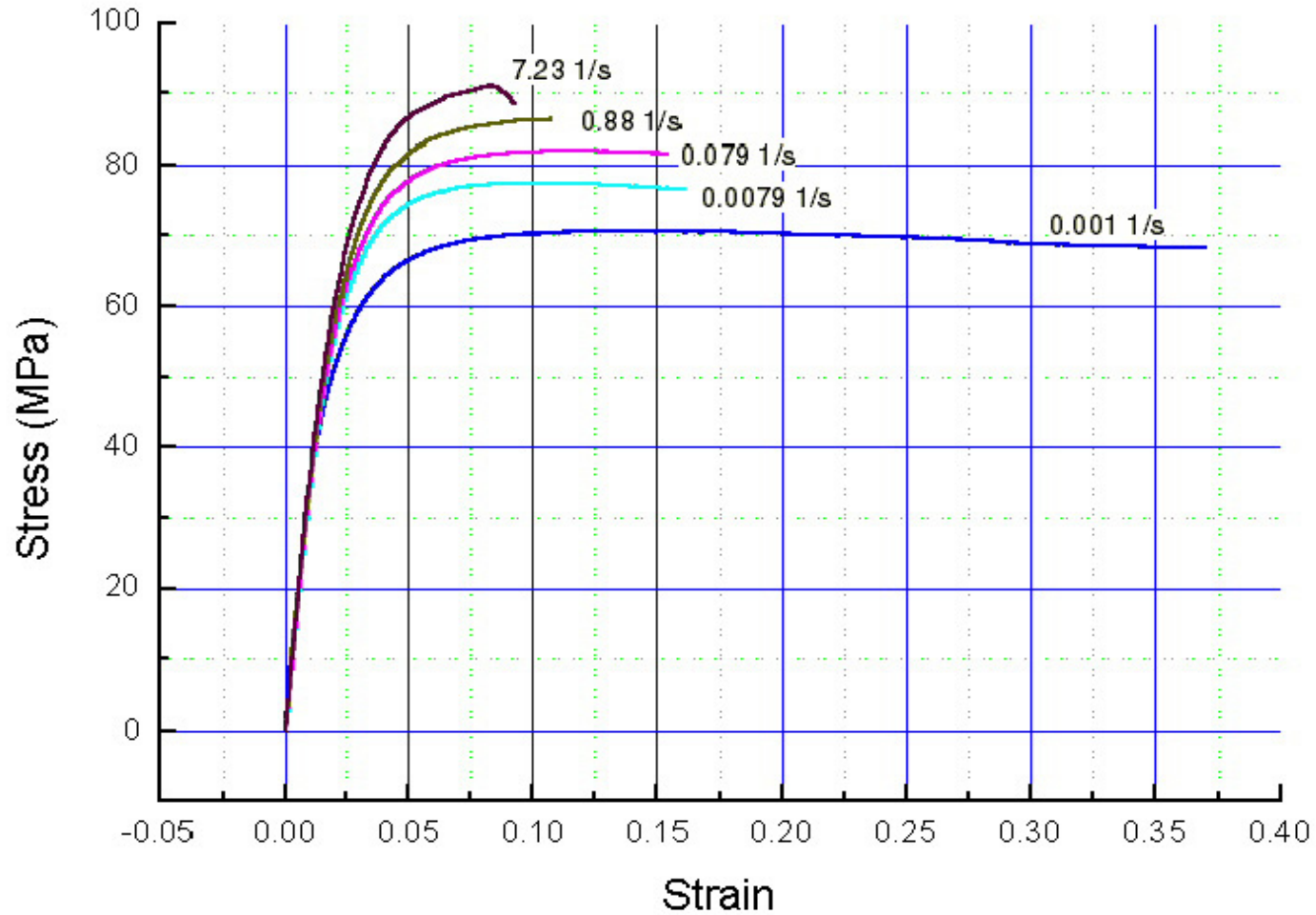




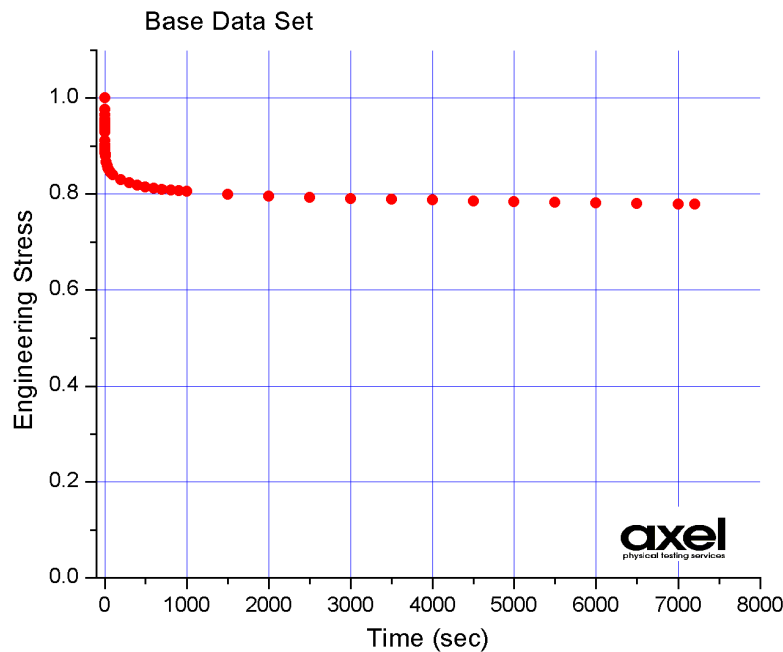
# Thermal Effects



# Rate of Loading



# Viscoelastic Behavior – Testing



## Viscoelastic Behavior

Can be Assumed to Reasonably  
Follow Linear Viscoelastic  
Behavior in Many Cases

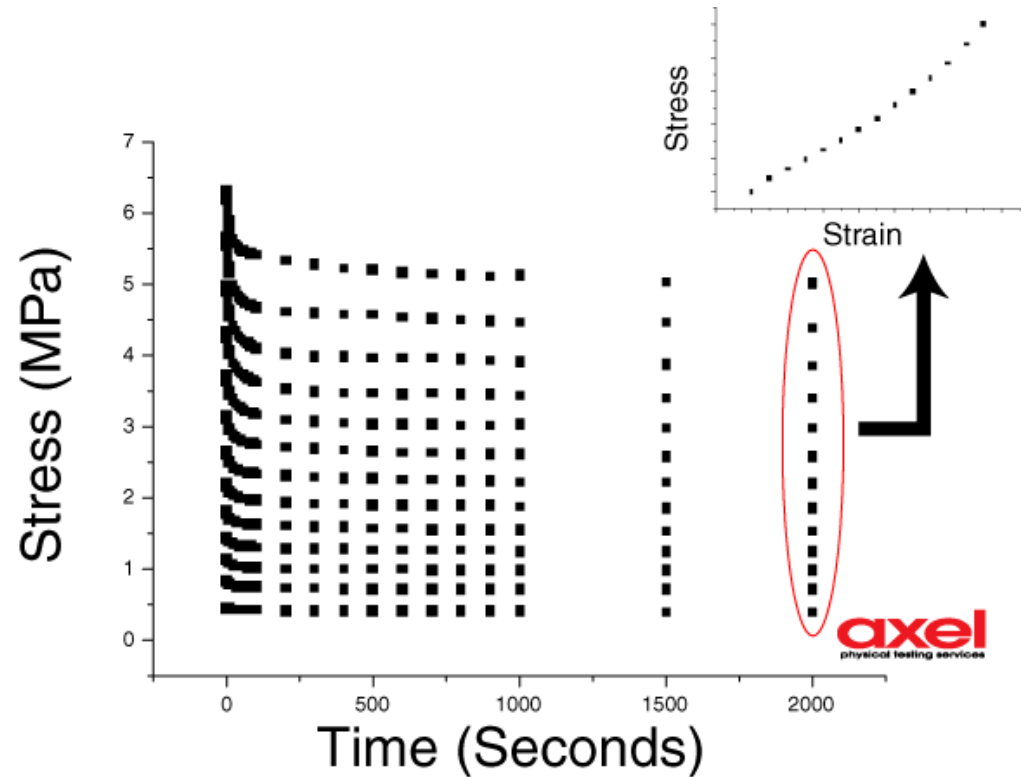
Is not the same as aging!

Describes the short term reversible  
behavior of elastomers.

Tensile, shear and biax have similar  
viscoelastic properties!

# Viscoelastic Behavior – Testing

A totally “relaxed” Stress-strain  
Curve can Be Constructed  
Decades of data in time are equally  
valuable for fitting purposes.

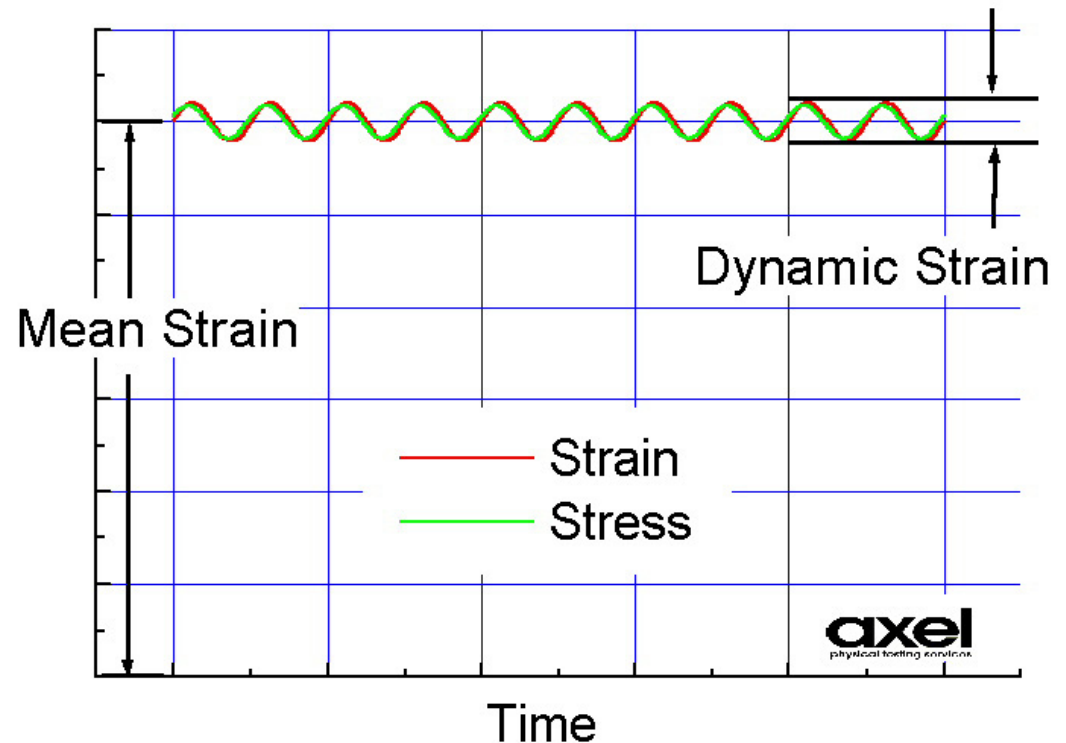


# Dynamic Behavior - Testing

Types of Dynamic Behavior

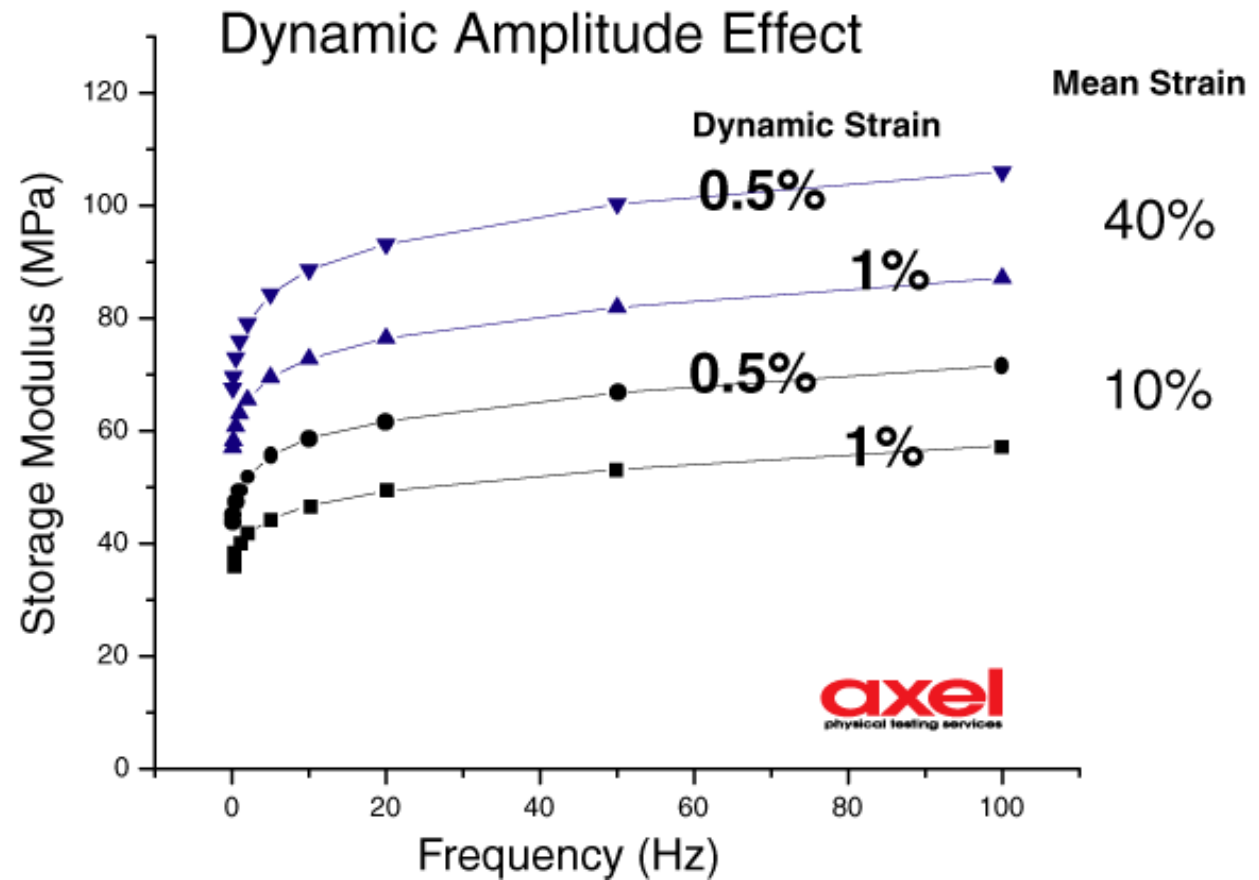
Large strains at high velocity

Small sinusoidal strains superimposed on large mean strains

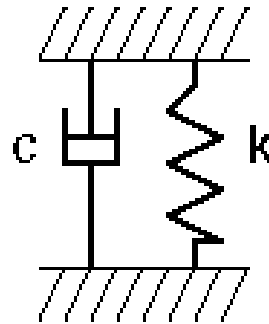
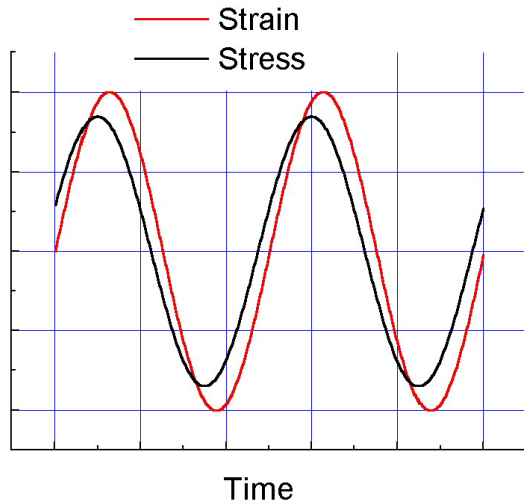


# Dynamic Behavior - Testing

Mean Strain and Amplitude  
Effects are Significant



# Low Speed Testing



**No inertia effect**

Long Wave Length vs Measurement

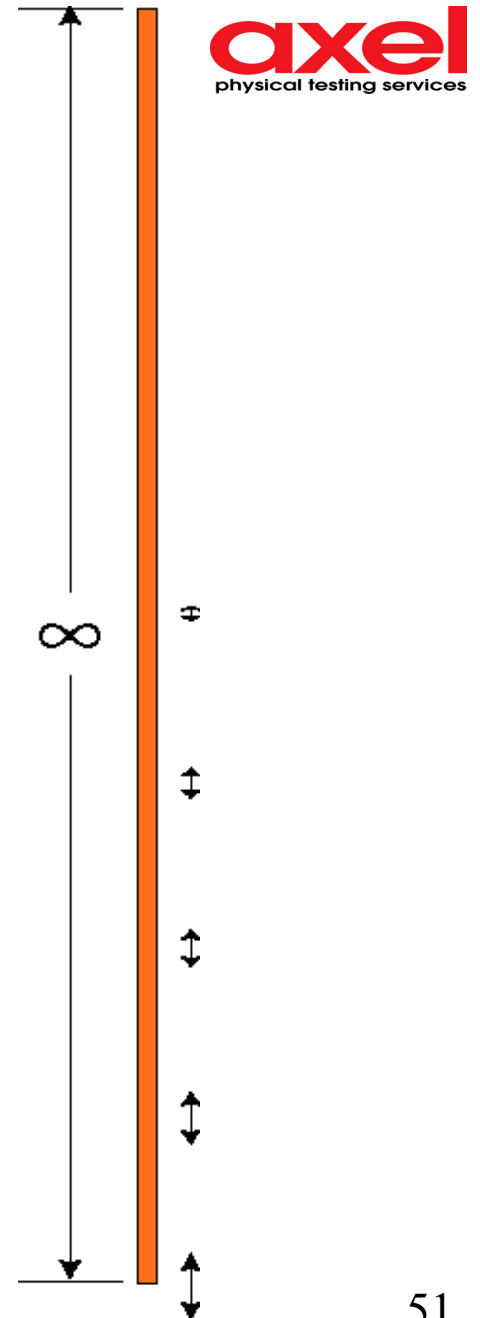
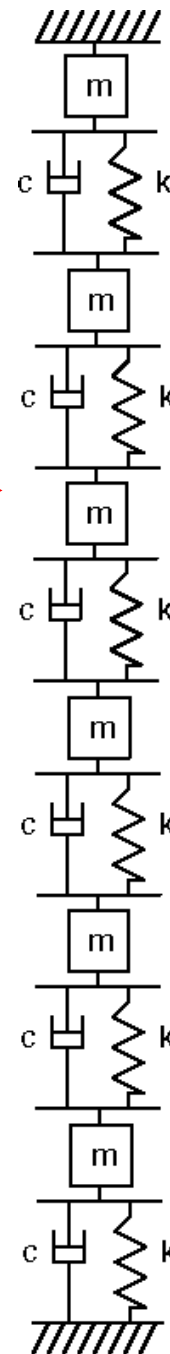
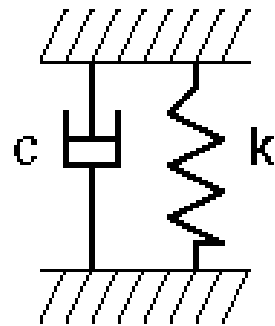
Dynamic Modulus = Peak Stress/ Peak Strain

Storage Modulus =  $E \cdot \cos \delta$

Loss Modulus =  $E \cdot \sin \delta$



# High Speed Dynamics



Wave Propagation

Inertial effect is Significant

Wave Length is Small

100 - 10,000 Hz.

# Wave Propagation

$$E^* = \rho c^2$$

Measure:

Density  $\rho$

Wave Speed  $c$

Wave Decay

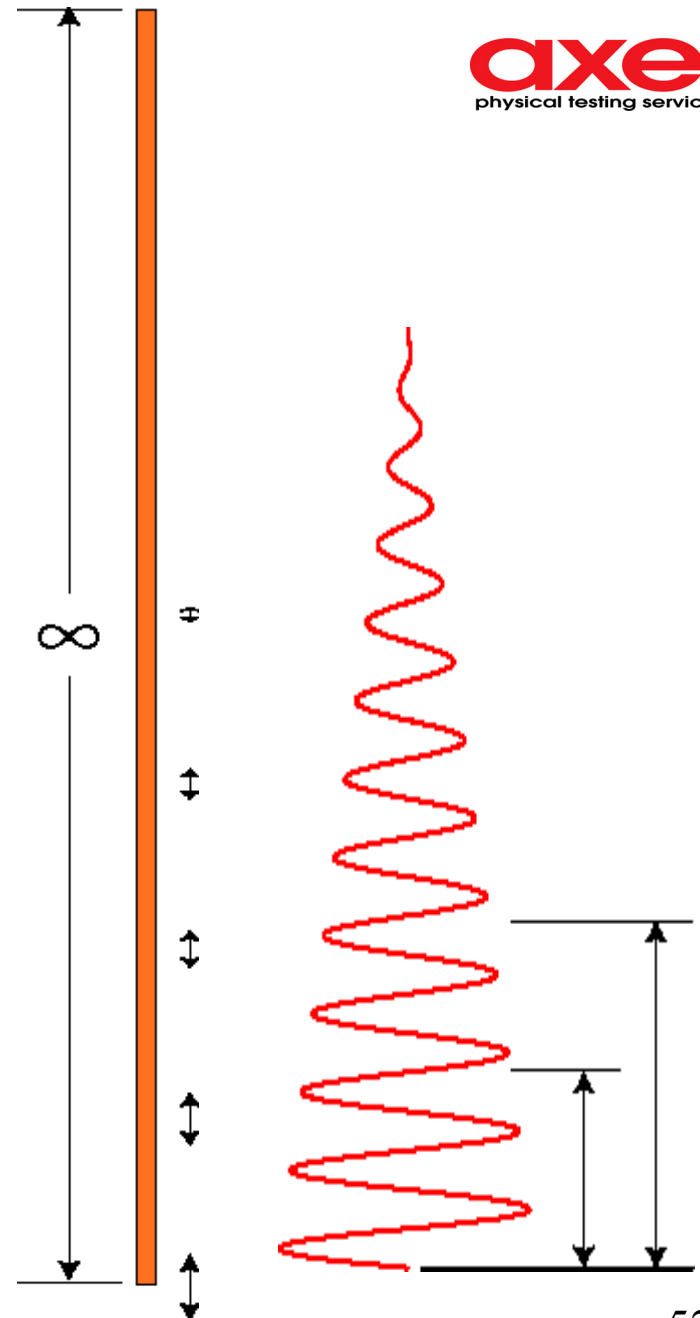
$$c = f\lambda$$

$c$  speed of longitudinal wave

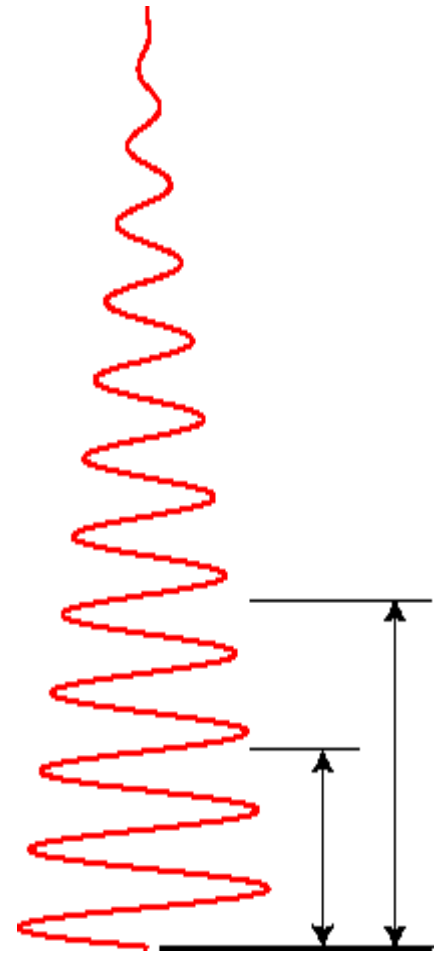
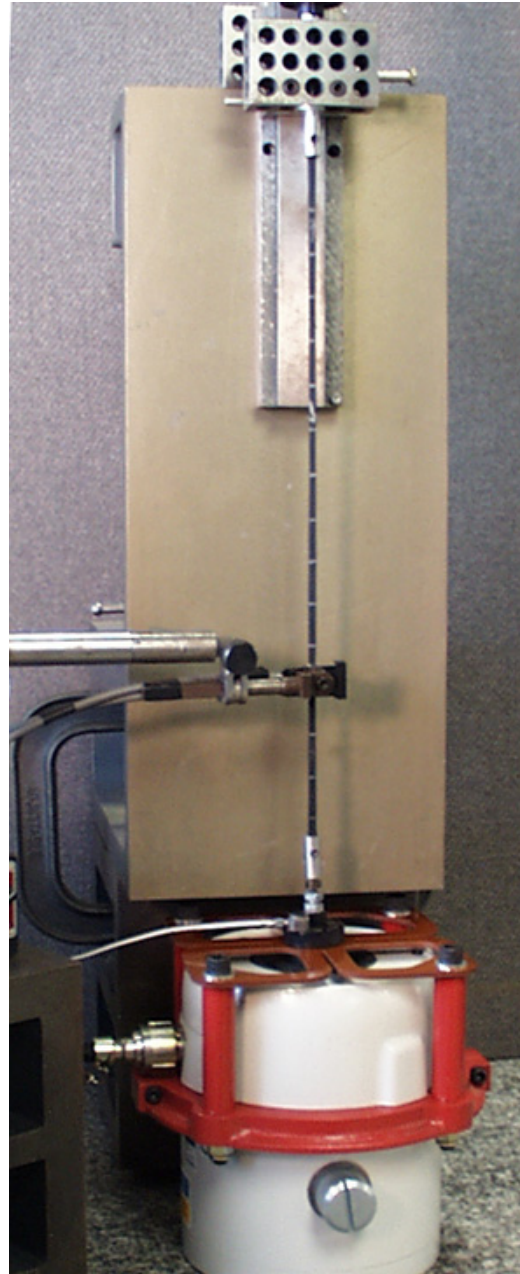
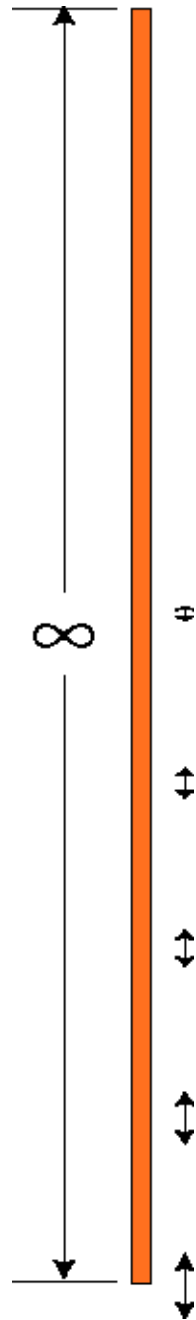
$f$  excitation frequency

$\lambda$  wave length

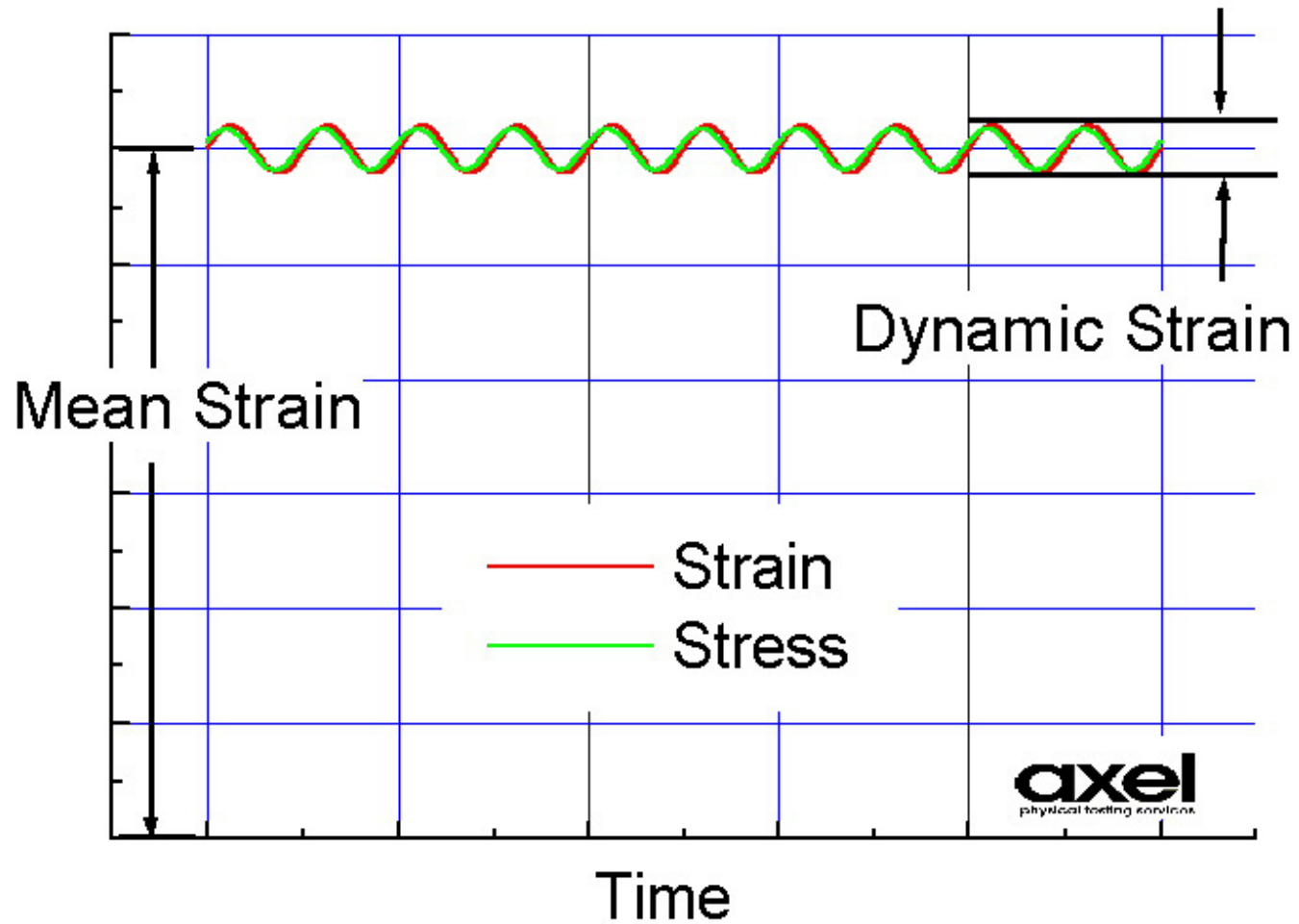
$E^*$  Dynamic Modulus



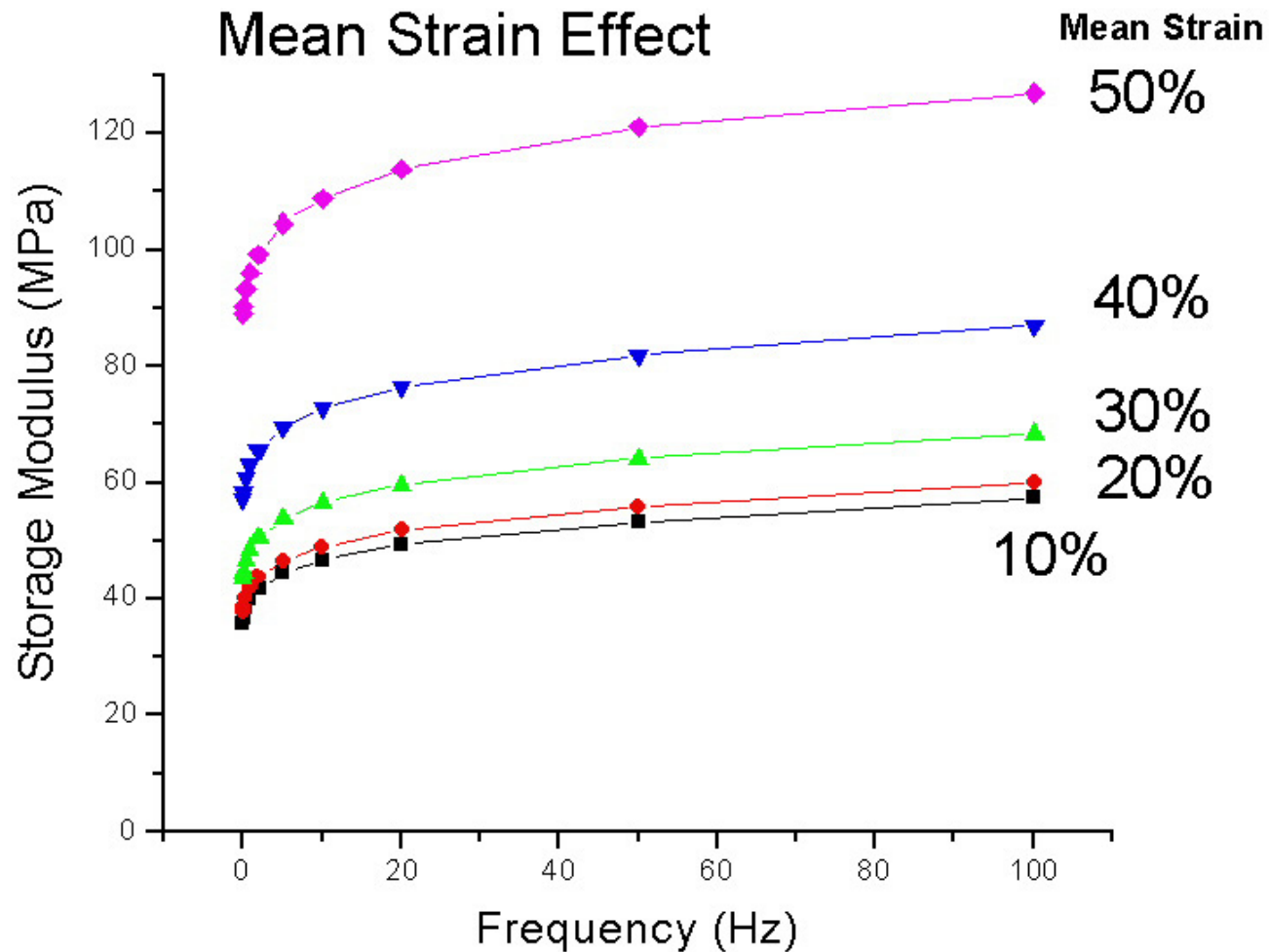
# Wave Propagation



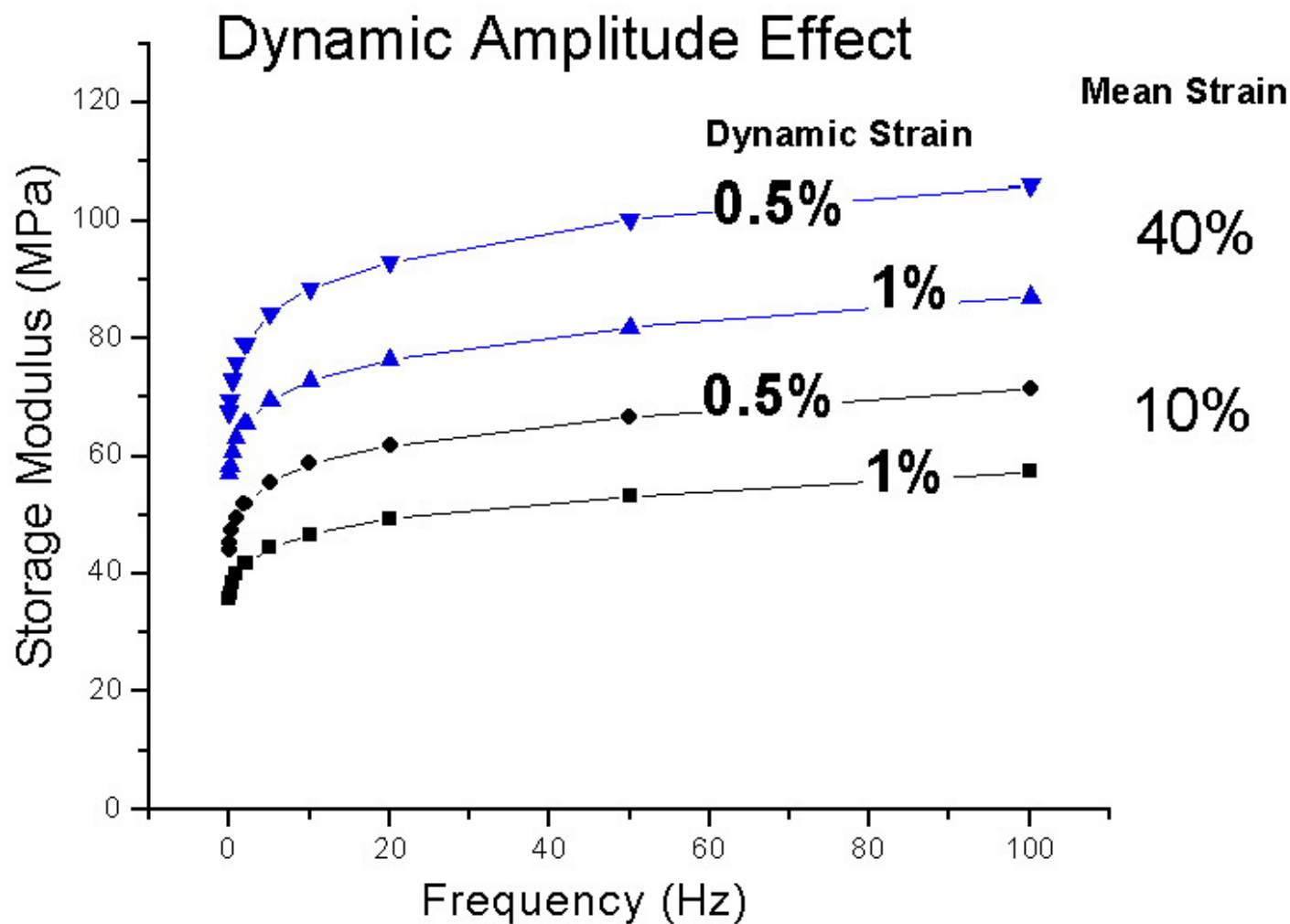
# Dynamic Vibrations



# Dynamic Vibrations

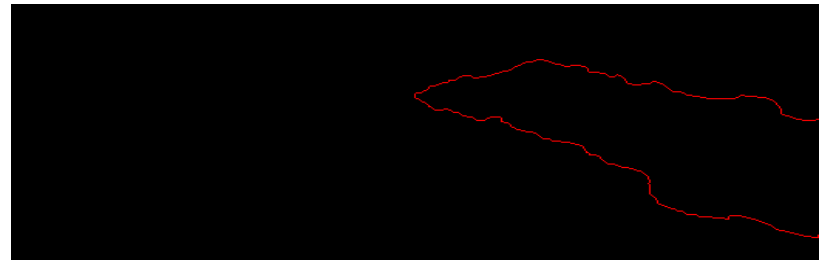
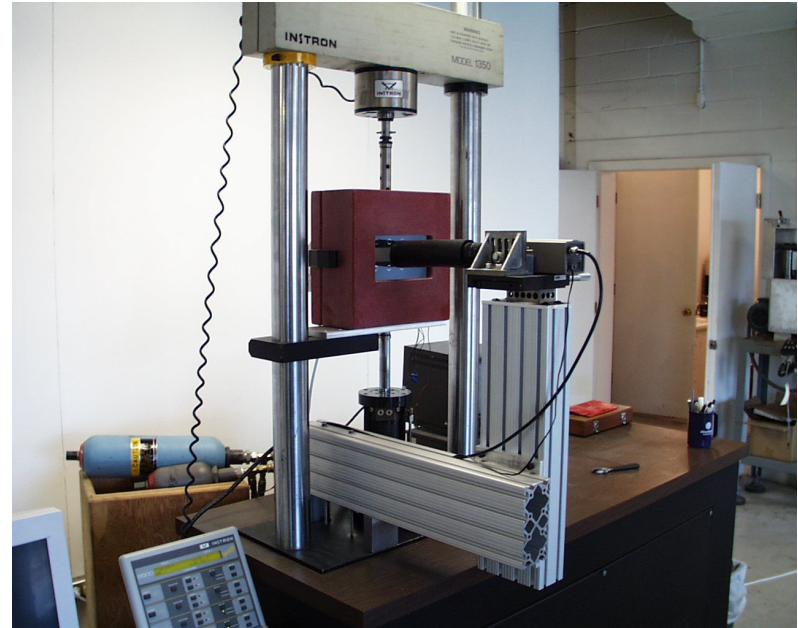
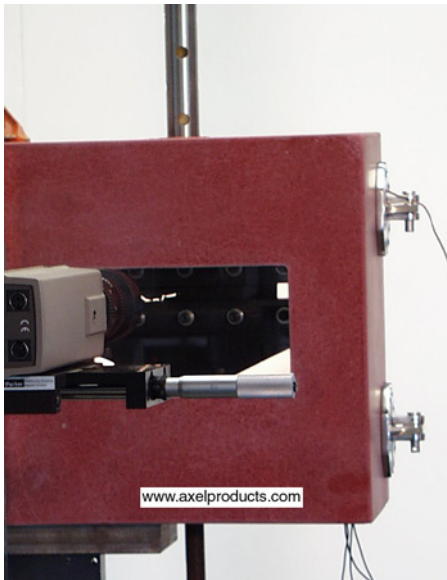


# Dynamic Vibrations



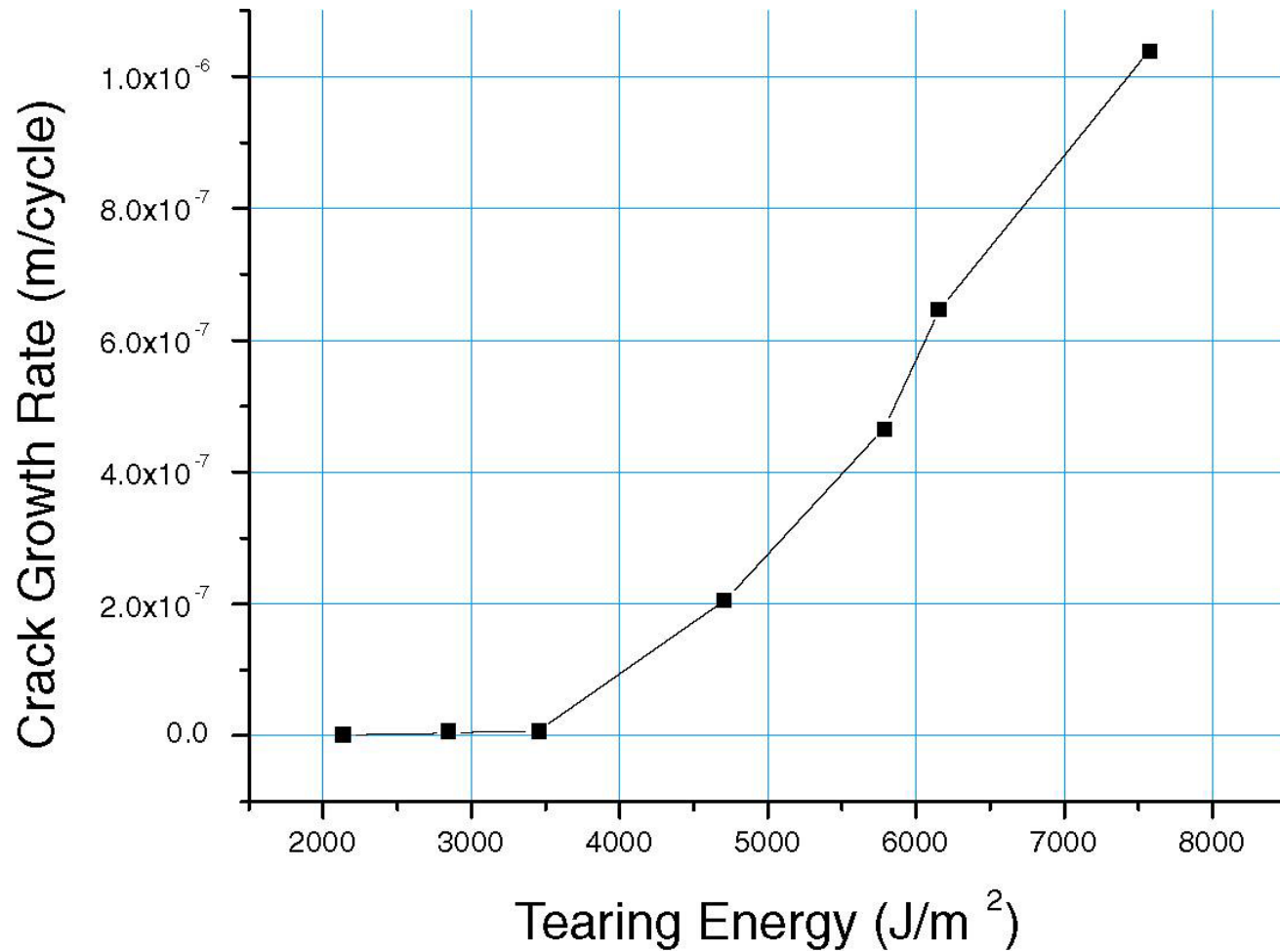
# Fatigue Crack Growth

Provides Great Potential.  
Not well understood.





# Fatigue Crack Growth



# Model Verification Experiments



## Attributes of a Good Model Verification Experiment

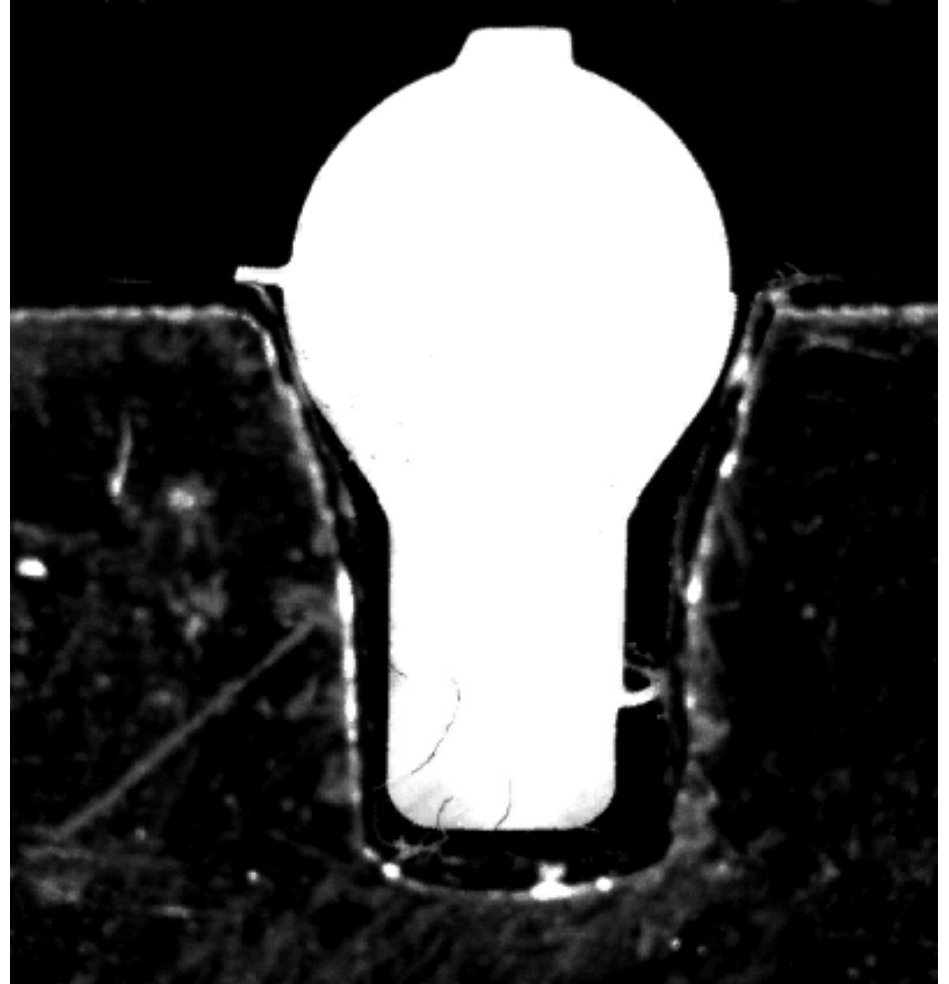
The geometry is realistic.

All Relevant Constraints are Measurable.

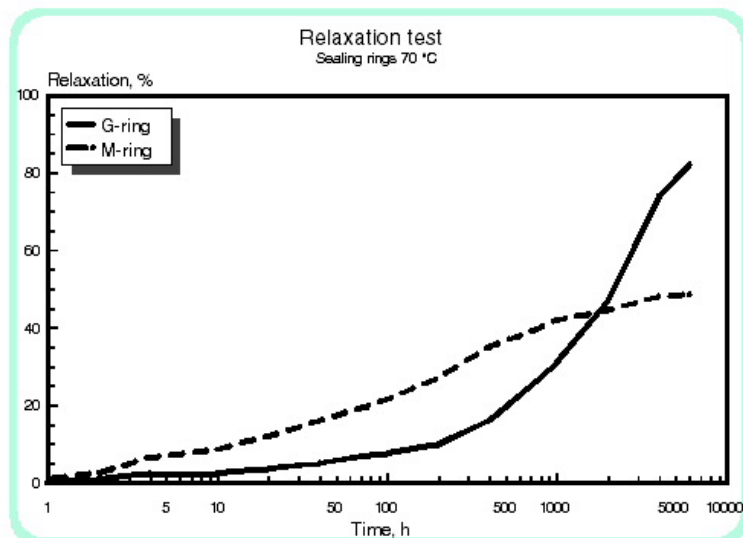
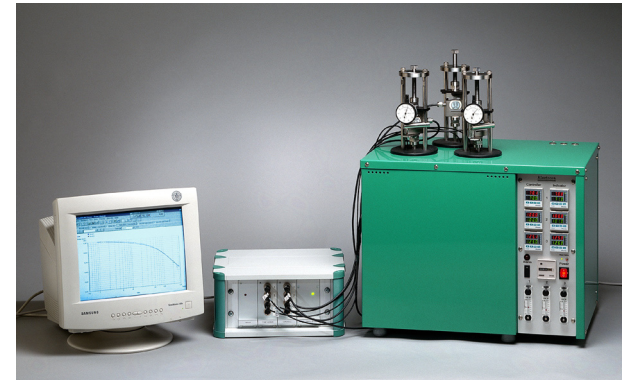
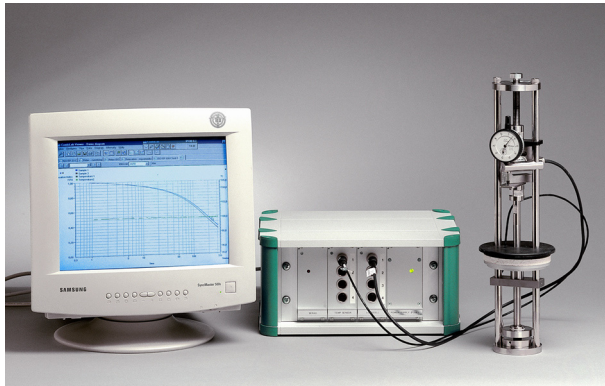
The Analytical Model is Well Understood

# Model Verification Experiments

The Contribution of the Flashing  
on the Part was Unexpected,  
Initially Not Modeled, But  
Very Significant to the  
Actual Load Deflection



# Thermal Aging



Elastoon AB

Relaxation:10 8/24/98

